

1 **Common species link global ecosystems to climate change**

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12 **Common species shape the world around us, and changes in their commonness signify**  
13 **large-scale shifts in ecosystem structure and function<sup>1-4</sup>. Dominant taxa drive**  
14 **productivity and biogeochemical cycling, in direct interaction with abiotic components**  
15 **of the Earth system<sup>3,4</sup>. However, our understanding of the dynamic response of**  
16 **ecosystems to global environmental changes in the past is limited by our ability to**  
17 **robustly estimate fossil taxonomic richness<sup>5,6</sup>, and by our neglect of the importance of**  
18 **common species. To rectify this, we use observations of the most common and**  
19 **widespread species to track global changes in their distribution in the deep geological**  
20 **past. Our simple approach is robust to factors that bias richness estimators, including**  
21 **widely used sampling-standardization methods<sup>5</sup>, which we show are highly sensitive to**  
22 **variability in the species-abundance distribution. Causal analyses of common species**  
23 **frequency in the deep-sea sedimentary record detect a lagged response in the ecological**  
24 **prominence of planktonic foraminifera to oceanographic changes captured by deep-**  
25 **ocean temperature records over the last 65 million years, encompassing one of Earth's**  
26 **major climate transitions. Our results demonstrate that common species can act as**  
27 **tracers of a past global ecosystem and its response to physical changes in Earth's**  
28 **dynamic history.**

29 True species richness can be elusive even in well-studied ecosystems, because most  
30 species are very rare, and relatively few species account for most of the total abundance<sup>1,2</sup>.  
31 For example, only ~1.4 % of the estimated tree species account for half of the biomass and  
32 control the cycling of water, carbon, and nutrients in the Amazon forest<sup>3</sup>. Similarly, a recent  
33 survey of eukaryotic diversity in the oceans found that ~0.24 % of the taxa accounted for half  
34 of the total number of rDNA reads<sup>4</sup>.

35 Abundance and occupancy are typically positively correlated, with the more abundant  
36 species being the more widespread<sup>4,7</sup>. In the fossil record, species and higher taxa generally

37 have a humped temporal distribution of occurrences, being rare in the early and late stages of  
38 their known stratigraphic range<sup>8-10</sup>.

39 Here we accommodate these ecological features by focussing only on species that are  
40 common and widespread at any given time, using the Summed Common species Occurrence  
41 Rate (SCOR), a very simple occurrence-based quantity that is sensitive to changes in total  
42 abundance (Methods)<sup>11</sup>. We apply SCOR to deep-sea sedimentary records of calcifying  
43 plankton (coccolithophores and foraminifera) over the last 65 years to demonstrate how  
44 relative changes in the distribution of common and widespread species were linked to climate  
45 change on geological time scales.

46 First, we evaluate the sensitivity of SCOR and commonly used richness estimators to  
47 potential biases using Poseidon, a simulation model of planktonic microfossil occurrences  
48 (Fig 1; Methods and Supplementary Code). We target methods currently popular in  
49 palaeobiology, and highlight the effects of two main factors: variability in the spatial  
50 sampling completeness (Fig. 1b), and variability in the shape of the species rank-abundance  
51 distribution (RAD; Fig. 1c).

52 Our simulations with Poseidon show that the SCOR estimate of relative changes in  
53 total abundance is highly robust to variability in both spatial sampling and RAD shape (Fig.  
54 1d). By definition, SCOR is immune to the loss of rare species, and decoupled from changes  
55 in richness. As expected, the fidelity of raw sampled richness (S) decays rapidly with  
56 increasing sampling variability, but shows little sensitivity to changes in the shape of the  
57 RAD. Simple range-through richness (RT; assuming a species existed in all time bins  
58 between its first and last occurrence) is relatively robust to both factors, indicating that the  
59 level of sampling in Poseidon is sufficient to avoid severe edge effects. The Shannon entropy  
60 H, which reflects both richness and evenness, is very sensitive to RAD shape variability,  
61 ultimately tracking changes in evenness at the expense of changes in richness. Classical

62 rarefaction (CR) and shareholder quorum subsampling (SQS)<sup>5</sup>, being sampling-  
63 standardization methods, are robust to the effect of spatial sampling variability on richness,  
64 all else being equal. However, both CR and SQS are highly sensitive to changes in RAD  
65 shape. As with Shannon H, increasing RAD variability causes CR and SQS to lose track of  
66 richness and respond to changes in the shape parameter  $\sigma$  of the RAD instead. Note that the  $\sigma$   
67 values used in Poseidon generally correspond to high, moderately variable species evenness  
68 (Supplementary Fig. 1). A third subsampling method, occurrences-squared weighted  
69 (O2W)<sup>12</sup>, shows overall poor agreement with true richness.

70 Turning to the rich deep-sea sedimentary record of the Cenozoic Era (0-65 million  
71 years ago), we analysed global occurrences of the two most prominent groups of calcifying  
72 plankton, coccolithophores and foraminifera, from the Neptune Sandbox Berlin (NSB)  
73 database<sup>13,14</sup> (Methods). In both groups, raw S generally increases along with the number of  
74 boreholes representing the spatial sampling, while sampled evenness (J) decreases  
75 (Supplementary Fig. 2a,b), as expected if improved sampling enhances the detection of rare  
76 species (Fig. 1b,c). Sampling-standardized richness estimates (SQS) seem to remove the  
77 sampling trend, but given the sensitivity of subsampling methods to RAD shape found in  
78 Poseidon, we suspected an evenness signal in the SQS estimates. Indeed, SQS richness can  
79 be reproduced by simply adding together the raw S and J curves (Supplementary Fig. 2c,d), a  
80 relationship that emerges across NSB data and simulation runs (Fig. 2). This result implies  
81 that changes in evenness are a major confounding factor for current sampling-standardized  
82 richness estimators.

83 Focussing instead on common species, coccolithophores and foraminifera have  
84 markedly different SCOR trajectories through the Cenozoic. On average, coccolithophores  
85 have their highest SCOR values in the Eocene, followed by a decline in the Oligocene and a  
86 resurgence in the late Miocene and Pliocene. Aspects of the coccolithophore SCOR pattern

87 have been linked to Cenozoic proxy records of atmospheric CO<sub>2</sub>, suggesting that  
88 coccolithophores could thrive in a high-CO<sub>2</sub> world<sup>11,15</sup>. Since their rise in the Mesozoic,  
89 coccolithophores shifted the dominant locus of carbonate burial from continental shelves to  
90 the deep sea, providing a new mechanism for buffering ocean chemistry and atmospheric  
91 CO<sub>2</sub> through carbonate compensation<sup>16</sup>. Oligocene cooling and CO<sub>2</sub> decline was  
92 accompanied by a lowering of the carbonate compensation depth, which has been attributed  
93 to changes in the supply of weathering products to the ocean<sup>17</sup>. The Oligocene reduction of  
94 coccolithophore SCOR is opposite to that expected if SCOR were biased upward by  
95 enhanced deep-sea preservation<sup>11</sup>, and carbonate preservation trends cannot explain the  
96 independent SCOR patterns in the two calcifying groups. Selective dissolution or taxonomic  
97 preferences in sample processing may cause short-term volatility in SCOR, but only if  
98 species presence or absence is random with respect to commonness (Supplementary Fig. 3).

99 Planktonic foraminifera SCOR was compared to Cenozoic deep-ocean temperature  
100 (DOT) records<sup>18</sup> (Methods; Supplementary Data Set). Although the net trends are inversely  
101 related (foraminifera flourish as the world cools), shorter-term changes suggest positive co-  
102 variation, including the Early Eocene climate optimum, Eocene cooling, as well as Miocene  
103 and Pliocene optima (Fig. 3a). Geological proxy records are generally noisy mixtures of  
104 signals representing multiple processes, derived from a sedimentary record that is itself an  
105 active component of the Earth system. Any causal connection detected between proxy  
106 records would necessarily be indirect with respect to the underlying processes of interest.  
107 Nonetheless, the DOT record reflects a set of climate-related variables, including changes in  
108 ocean thermohaline circulation, water mass structure, and nutrient dynamics, all considered  
109 to be important abiotic controls on the long-term evolution of planktonic foraminifera<sup>6,19-21</sup>.  
110 Here we tested this drive-response hypothesis using three conceptually very different  
111 methods for causal detection in time series (Methods): (1) Convergent cross mapping<sup>22</sup>, based

112 on the concept of state space reconstruction from time-delay embedding; (2) Information  
113 transfer analysis<sup>23,24</sup>, based on the concept of transfer entropy<sup>25</sup>; and (3) Bayesian inference  
114 of causal models based on linear stochastic differential equations<sup>26,27</sup>.

115 Convergent cross mapping (CCM) from foraminifera SCOR to DOT peaks at a  
116 negative lag, indicating that the SCOR signal carries a response to past changes captured in  
117 the DOT record (Fig. 3b). The optimum lag is a single time bin, implying a causal delay of  
118 0.5 million years (Myr) or less. CCM is also significant in the opposite direction but this is  
119 stronger at positive lags (Fig. 3b), which are non-causal (future "drives" past). This result is  
120 consistent with a unidirectional forcing where the dynamics of the response variable (SCOR)  
121 is dominated by the driving variable (DOT), such that predictability flows both ways<sup>28</sup>.  
122 Information transfer (IT) analysis supports this inference: predictive information flow is  
123 significant from past DOT to SCOR, although the optimal lag is shifted backward by one  
124 time bin, implying a more protracted causal delay (Fig. 3c). In the opposite direction, IT  
125 peaks at the corresponding positive (non-causal) lags, but is significantly weaker than in the  
126 causal direction. Using a series of linear Stochastic Differential Equations (SDEs) to model  
127 correlation and causality between the two records (Supplementary Fig. 4), we recover  
128 relatively strong evidence that SCOR responds to changes in DOT, with a time lag of 0.33-  
129 1.1 Myr, comparable to the CCM and IT analyses (Supplementary Tables 1, 2), although the  
130 detailed nature of the causal relationship cannot be clearly resolved (Methods).

131 The congruence of these results strongly suggests that the ecological prominence of  
132 planktonic foraminifera has evolved in response to past climatic and oceanographic changes  
133 captured in the deep-ocean temperature proxy record. Furthermore, the inferred time delay  
134 implies that the causal connection is highly indirect, involving climate changes propagating  
135 through the Earth system to influence the commonness of foraminifera in the global plankton  
136 on evolutionary time scales. In the modern global ocean, eukaryotic plankton richness

137 involves a vast number of parasite and symbiont species, highlighting the importance of  
138 biotic interactions in driving diversification through trophic connectivity and complexity<sup>4</sup>.  
139 Abiotic factors, such as differences in nutrient level among ocean basins, are more clearly  
140 reflected in the relative abundance of the dominant species. A restructuring of water masses  
141 and nutrient distributions is likely to cause a dramatic and discernible shift in the distribution  
142 and abundance of many species, yet have a far less predictable impact on richness. Our  
143 results imply that if such a fundamental ecosystem response were to leave a signature in the  
144 fossil record, it would be far more evident in the robustly detectable distribution of the most  
145 common species than in the indeterminate richness of rare species. Dominant groups also  
146 reveal macroevolutionary trends in functional morphology otherwise obscured by rare taxa<sup>29</sup>.  
147 Given their critical importance to ecosystem functioning, common species provide a nexus  
148 for understanding the role of an evolving biota in global environmental changes of the past.

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217

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226 **Author Contributions** B.H. and L.H.L. designed the study. B.H. ran the Poseidon

227 simulations, analysed data, performed the IT analysis, and wrote the paper. L.H.L. retrieved

228 the NSB data, calculated SCOR, and wrote the Poseidon code. K.A.H. and D.D. performed

229 the CCM analysis. T.R. performed the SDE analysis. All authors discussed the results and

230 commented on the manuscript.

231

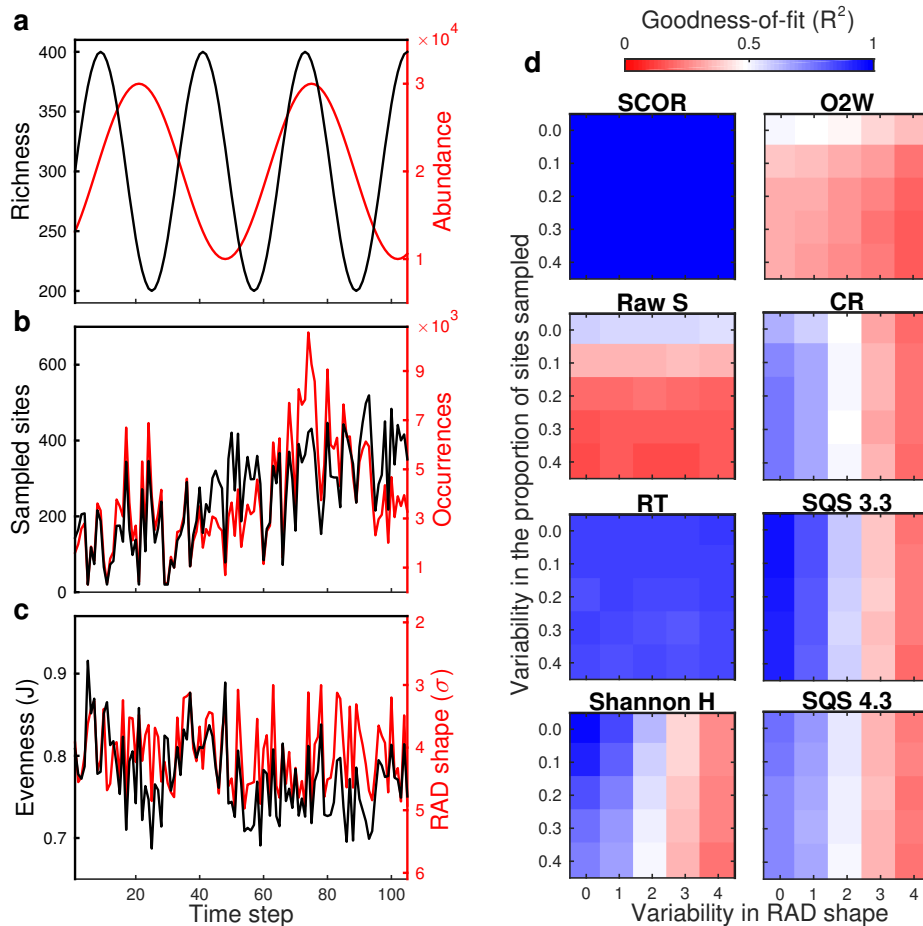
232 **Additional Information** Supplementary information is available in the online version of the

233 paper. Reprints and permissions information is available at [www.nature.com/reprints](http://www.nature.com/reprints).

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239 **Figure 1 | Performance of SCOR and richness estimators in Poseidon model**

240 **experiments. a**, Simulated species richness and total abundance are decoupled. **b**, Sampled

241 species occurrences reflect abundance distorted by the trend and short-term variability in

242 sampled sites (in this example, variability = 0.1, corresponding to the standard deviation

243 around the mean trend). **c**, Sampled species evenness (Pielou's J) captures changes in the

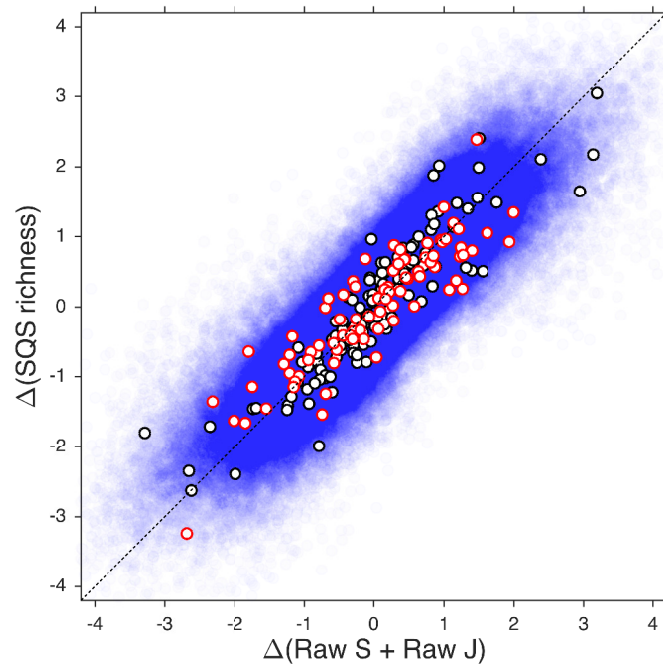
244 shape parameter  $\sigma$  of the RAD (in this example, variability = 2, corresponding to the range of

245  $\sigma$ ), superimposed on richness fluctuations and a net decrease caused by the sampling trend. **d**,

246 Sensitivity to sampling variability and RAD shape variability. Values are median goodness-

247 of-fit ( $R^2$ ) of 50 model runs, comparing SCOR to true abundance, and richness estimates to

248 true richness. See text for abbreviations.



249

250 **Figure 2 | Empirical relationship between sampling-standardized richness and the sum**

251 **of raw richness and evenness.** Values are first differences of normalized time series of SQS

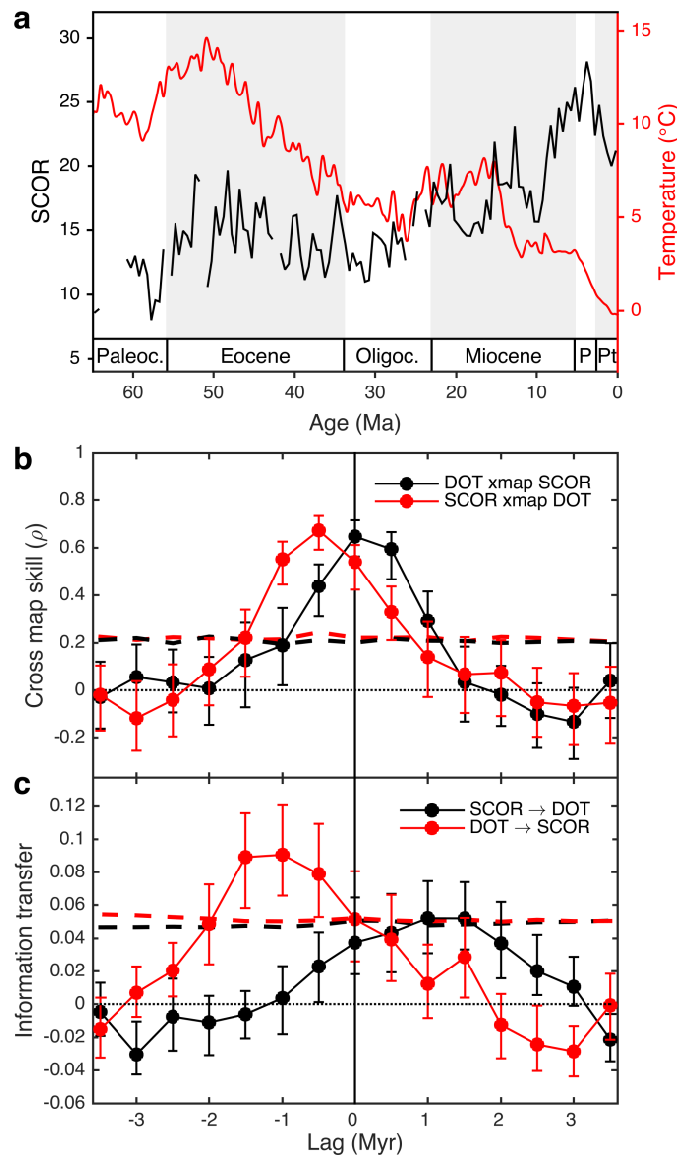
252 richness and of the sum of normalized raw richness (S) and evenness (Pielou's J). Data

253 include Cenozoic coccolithophores (black) and planktonic foraminifera (red) from the NSB

254 database (Supplementary Fig. 2), and all Poseidon model experiments (blue;  $N = 262,500$ ).

255 Stippled line marks the 1:1 relationship.

256



257

258 **Figure 3 | Testing a causal link between planktonic foraminifera SCOR and Cenozoic**

259 **climate changes. a**, SCOR of planktonic foraminifera from the NSB database at 0.5 Myr

260 resolution, and DOT estimates<sup>18</sup> at 0.1 Myr resolution. **b, c**, CCM skill (**b**) and IT (**c**) between

261 SCOR and DOT as a function of time lag. If past DOT drives SCOR, then SCOR *xmap* DOT,

262 while information flows DOT  $\rightarrow$  SCOR, at negative lags. Values are medians (dots) and 95

263 % ranges (whiskers) for 500 random subsamples of length 100, dashed lines are 95<sup>th</sup>

264 percentiles of 1,000 surrogates. All values are normalized to a surrogate mean of zero. Ma,

265 million years before present; Paleoc., Paleocene; Oligoc., Oligocene; P, Pliocene; Pt,

266 Pleistocene.

267 **METHODS**

268 **Data.** Microfossil occurrences were retrieved from the NSB database<sup>13,14</sup> (accessed April 22,  
269 2015). SCOR and richness estimates were calculated using 0.5 Myr time bins. For the  
270 planktonic foraminifera, we compared the inferred times of species rise and fall in NSB<sup>10</sup>,  
271 which encompass any period of potential commonness, to the species ranges in the  
272 PlankRange database<sup>30</sup> (<http://palaeo.gly.bris.ac.uk/Data/plankrange.html>, accessed Aug. 24,  
273 2014). After resolving most of the taxonomic discrepancies, ~82 % of the species have a rise-  
274 fall interval that fits within the proposed range or is offset by < 2 Myr (a single time bin in  
275 ref. 10). Of the remaining species, which could either not be matched taxonomically or have  
276 a significant range offset, ~73 % are rare (peak occurrence frequency, as a proportion of all  
277 sites with at least one species sampled, < 0.2), and none have a peak occurrence frequency >  
278 0.4. Taxonomic or range errors in NSB are therefore unlikely to have a significant impact on  
279 SCOR, which is sensitive only to the most widespread species. Quantification of this impact  
280 awaits the public release of the updated PlankRange database<sup>31</sup>.

281 DOT estimates were obtained from ref. 18, using their > 9 Ma  $T_{d-SL}$  record (based on  
282 subtracting New Jersey sea level records from a benthic  $\delta^{18}O$  stack) and scaled  $\delta^{18}O$  record  
283 for the interval < 9 Ma, with their interpolation at 0.1 Myr resolution. Both SCOR and DOT  
284 were tied to the GTS2004 time scale<sup>32</sup>.

285 **SCOR.** We treat the observation of a specific number of individuals as a Poisson-distributed  
286 variable with parameter  $\lambda$  in each time bin. The probability of finding an individual of species  
287  $i$  in time bin  $j$  is then  $p_{ij} = 1 - \exp(-\lambda_{ij})$ , and thus  $\lambda_{ij} = -\ln(1 - p_{ij})$ . In practice,  $p_{ij}$  is estimated  
288 as  $y_{ij}/n_j$ , where  $y_{ij}$  is the number of sites in which species  $i$  is observed at time bin  $j$  and  $n_j$  is  
289 the number of sites in that time bin where at least one of the species included in the analysis  
290 is observed. SCOR is the total density of a given set of  $m_j$  species in a time bin:

291 
$$SCOR_j = \sum_{i=1}^{m_j} \lambda_{ij} \quad (1)$$

292 and we estimate its variance by the delta method<sup>33</sup>:

293 
$$Var(SCOR_j) = \sum_{i=1}^{m_j} \frac{p_{ij}}{(1 - p_{ij})n_j}. \quad (2)$$

294 SCOR is based on the observation that the more globally abundant a species is, the more  
295 likely it is to occur at a greater number of sites<sup>4</sup>. As  $p$  approaches 1, the rate of increase in  $\lambda$   
296 grows rapidly, such that very widespread species have a much greater influence on SCOR  
297 than restricted species. If a species occurs at all sites in a time bin, its  $\lambda$  for that time bin is  
298 undefined.

299 SCOR is decoupled from species richness and relative abundance. If a species  
300 becomes globally more abundant and widespread in a time interval, then its  $\lambda$ , and thus  
301 SCOR, will increase. Even if all species became exactly equally more common in absolute  
302 terms, with no change in relative abundance, their individual  $\lambda$  values will be higher and  
303 SCOR will capture the proportional change in absolute abundance of the total species set.

304 **Poseidon simulations.** To evaluate the performance of SCOR relative to commonly used  
305 diversity metrics, we designed a set of numerical experiments on the effects of temporal  
306 variability in three factors: (1) spatial sampling completeness; (2) the shape of the species  
307 rank-abundance distribution (RAD); and (3) the proportion of species lost randomly (with  
308 respect to abundance).

309 Poseidon consists of 1,000 spatial grid cells and 105 time steps, where true species  
310 richness and abundance are allowed to vary independently (Fig. 1a). In each time step, we  
311 randomly assign an abundance value to each species, such that the entire community has a  
312 log-normal rank-abundance distribution (RAD), the shape of which can be fixed or time-  
313 varying. Species ranks are randomly reshuffled between time steps. We then randomly assign

314 a spatial grid cell (site) to an individual of a species, where it can potentially be preserved and  
315 sampled.

316 Next, we sample only a proportion of the sites (spatial cells) such that this proportion  
317 increases linearly from 0.1 to 0.4, representing a declining sampling coverage with age,  
318 typical of deep-sea sedimentary records. Any short-term variability is thus superimposed on  
319 this trend (e.g. Fig. 1b). Furthermore, a proportion of the remaining species can be randomly  
320 removed (representing dissolution, selective picking, or other processes causing a species to  
321 be absent in a time bin, regardless of its original abundance).

322 We then calculate raw S, RT, Shannon H, and three sampling-standardized richness  
323 metrics widely used in palaeobiology (CR, O2W, and SQS). Although a generalized OXW  
324 has been recommended for paleontological datasets<sup>34</sup>, we use O2W here because our data  
325 meet the assumptions of the latter<sup>12</sup>. We used two versions of the shareholder quorum  
326 subsampling (SQS) method<sup>5,35-37</sup>: the SQS3.3 R script  
327 (<http://bio.mq.edu.au/~jalroy/SQS.html>, downloaded Aug. 26, 2014), and the SQS4.3 perl  
328 script, kindly provided by J. Alroy (Sept. 3, 2014). We did not modify the SQS codes but  
329 wrote a function to format Poseidon output to species occurrence data for SQS4.3. For  
330 SQS3.3, we input the list of sampled individuals (abundances). A quorum level of 0.6 was  
331 used in all runs. Both SQS versions yielded very similar results when given the same type of  
332 data (abundances or occurrences). For all subsampling methods (CR, O2W, and SQS), 100  
333 iterations were used in obtaining each estimated richness value. Increasing the number of  
334 iterations offered no discernible improvement. Shannon H was output from the SQS 3.3 R  
335 script and used to calculate Pielou's J evenness. The goodness-of-fit between true and  
336 estimated richness, and between true abundance and SCOR, was assessed by the coefficient  
337 of determination ( $R^2$ ) between time series. Poseidon R scripts are provided as Supplementary  
338 Code.



339 **Time Series Analysis.** We used three different time series analysis methods to test for a  
340 causal relationship between SCOR and DOT. Two of the methods are non-parametric, while  
341 the third is based on linear models. To implement a time-displacement (lag) analysis for the  
342 non-parametric methods, missing SCOR values were linearly interpolated, and the 0.1-Myr  
343 resolution DOT record was bin-averaged on the SCOR time bins (0.5 Myr). Furthermore, the  
344 non-parametric methods use surrogate time series to assess significance, which requires  
345 detrending of the original time series. To avoid any bias from differences in non-stationarity  
346 that are not reproduced by the surrogates, both records were detrended using a third-order  
347 polynomial to satisfy a stationarity criterion<sup>38</sup>, then normalized to zero mean and unit  
348 standard deviation. For consistency, the model-based analysis was also performed on the pre-  
349 processed data. However, the detrending may remove components of the variation relevant to  
350 uncovering the parameters of underlying processes. We therefore repeated the model-based  
351 analysis on untransformed data.

352 **CCM analysis.** CCM is a method for causal inference in nonlinear dynamical systems based  
353 on the theory of state-space reconstruction<sup>22</sup>. Consider two time series  $X$  and  $Y$  consisting of  
354 scalar observations of variables in a dynamical system. According to Takens's theorem<sup>39</sup>, we  
355 can construct a delay-coordinate embedding of the state space of the dynamical system into  
356 an  $m$ -dimensional real space, by constructing the vectors  $E_X = \{ \{ x(t_i), x(t_i - \tau), x(t_i - 2\tau), \dots,$   
357  $x(t_i - (m\tau)) \} \}$ , where  $x(t_i)$  is the scalar value of the time series  $X$  at time  $t_i$ . That is, the vectors  
358 in  $E_X$  are in one-to-one correspondence with the states of the dynamical system. If  $X$  and  $Y$   
359 are coupled variables of the same dynamical system (i.e. they are causally influencing each  
360 other), this correspondence is also true for time series  $Y$ , and therefore  $E_X$  and  $E_Y$  are in one-  
361 to-one correspondence with each other. CCM uses this result to predict scalar values of  $Y$   
362 from the coordinate-delay embedding of  $X$  and vice versa.

363 The CCM algorithm locates, for each scalar point  $P_i$  in the prediction set (subset of  
364 time series  $Y$ ), the contemporaneous state vector  $L_i$  in the library set (subset of state vectors in  
365 the time-delay embedding constructed from time series  $X$ ). Next, it finds  $L_i$ 's closest  
366 neighbours and estimates a value for the predictee  $P_{i*}$  using simplex projection<sup>40</sup>. CCM skill  
367 is determined by the correlation (Pearson's  $\rho$ ) between estimated  $P_{i*}$  and actual values of  $P_i$ .  
368 With increasing library size, CCM skill is expected to increase and converge if the variables  
369 are causally related. The notation " $X$  xmap  $Y$ " refers to estimating  $y(t_i)$  from corresponding  
370 lagged-coordinate state versions of  $x(t_i)$ , which in a causal context is read as " $Y$  is causally  
371 influencing  $X$ ".

372 CCM analysis was performed using the rEDM software package<sup>41</sup>. We constructed  
373 time-delay embeddings using embedding dimension  $m = 2$  and delay time step  $\tau = 1$ . Cross  
374 mapping was then performed using the entire time series as both prediction and library sets.  
375 To avoid biased results, we used leave-one-out cross validation (i.e. the predictee  $P_i$  itself and  
376 points in a time radius of  $E$  around  $P_i$  were excluded from the libraries, such that no points  
377 sharing coordinates with  $P_i$  were used in the predictions; see refs. 41, 42).

378 If unidirectional forcing is sufficiently strong, the dynamics of the response variable  
379 can become dominated by the driving variable. In this case, CCM may be significant in both  
380 directions, and thus unable to distinguish unidirectional forcing from bidirectional causality.  
381 To address this, we used the extended CCM approach<sup>28</sup>, which repeats the cross mapping  
382 using different time-displacements of the original time series. If there is a discernable lag  
383 between cause and effect, then optimal cross map skill is expected to occur for negative time  
384 lags in the direction(s) of true causality (past drives future). If true causality is unidirectional,  
385 then any CCM skill in the non-causal direction is expected to peak for positive lags (future  
386 "drives" past).

387 Extended CCM analysis of SCOR and DOT is reported as median cross map skill and  
388 95 % ranges at different lags after drawing 500 samples with replacement from libraries of  
389 size 100. Statistical significance is evaluated against a null distribution of CCM results for  
390 1000 surrogate time series. For each lag, CCM skill is considered significant if it exceeds the  
391 95<sup>th</sup> percentile of the surrogates. We verified the results using three different methods for  
392 generating surrogate data: phase-randomized and amplitude-adjusted Fourier transform  
393 (AAFT)<sup>43</sup>, phase-randomized Fourier transform<sup>44</sup>, and randomly shuffled surrogates. All  
394 three methods indicate significant causality from DOT to SCOR, and we limit our results to  
395 the AAFT method, which gave the most conservative significance estimates.

396 **IT analysis.** If two processes  $X$  and  $Y$  are independent, then a general Markov property will  
397 hold<sup>25</sup>:

$$398 \quad p(x_{n+1} | x_n^{(k)}, y_n^{(l)}) = p(x_{n+1} | x_n^{(k)}), \quad (3)$$

399 where  $p(x_{n+1})$  is the transition probability to state  $n+1$ , and indices  $k$  and  $l$  are the dimensions  
400 of vectors of past states. In the absence of information flow from  $Y$  to  $X$ , knowing the past  $l$   
401 states of  $Y$  has no influence on the transition probability of  $X$  beyond knowing the past  $k$   
402 states of  $X$  alone. Transfer entropy<sup>25</sup> quantifies the incorrectness of assuming independence  
403 by means of a Kullback-Leibler divergence, a non-symmetric measure of the information lost  
404 when the right hand side is used to approximate the left hand side of equation (3):

$$T_{Y \rightarrow X} = \sum_{x,y} p(x_{n+1}, x_n^{(k)}, y_n^{(l)}) \log \frac{p(x_{n+1} | x_n^{(k)}, y_n^{(l)})}{p(x_{n+1} | x_n^{(k)})} \quad (4)$$

405 Transfer entropy is thus a non-symmetric measure of information flow, which has been  
406 shown to be equivalent to a conditional mutual information<sup>45</sup>, and equivalent to Granger  
407 causality<sup>46</sup> for linear, Gaussian systems<sup>47</sup>. We implement it in the modified IT form proposed  
408 by Verdes<sup>23</sup>, which has previously been applied to the analysis of geological records<sup>11,24,48,49</sup>.

409 Here we expand on these earlier applications by repeating the IT analysis for different  
410 time-displacements of the original time series, analogous to the extended CCM analysis  
411 described above. Similar to CCM, predictive information flow may become symmetric if  
412 unidirectional forcing and/or linear correlation is sufficiently strong. However, if there is a  
413 discernable lag between cause and effect, then optimal information transfer is expected to  
414 occur for negative time lags in the direction(s) of true causality (past  $\rightarrow$  future). If true  
415 causality is unidirectional, then any information flow in the non-causal direction is expected  
416 to peak for positive lags (future  $\rightarrow$  past). IT is a coarse-grained relative entropy measure,  
417 which varies as a function of the data gridding resolution, summarized in a single IT value as  
418 the area under the resulting curve<sup>23</sup>. Lagged IT analysis of SCOR and DOT is reported as  
419 median IT and 95 % ranges at different lags after drawing 500 random subsamples of size  
420 100. IT is considered significant if it exceeds the 95<sup>th</sup> percentile of a null distribution of IT  
421 results for 1,000 AAFT surrogate time series. Unlike CCM, this IT implementation does not  
422 use time-delay embedding. Combined with coarse-graining of the data, this may help explain  
423 the difference in optimal lag between IT and CCM (Fig. 3b, c), although more work is needed  
424 to clarify this.

425 **Linear SDE analysis.** Given two time series representing two measured processes, linear  
426 SDEs can be used to distinguish between correlation and Granger causality. Uni- and  
427 bidirectional causation as well as hidden (unmeasured) processes can be modelled in the SDE  
428 framework, expanding the space of possible connections<sup>26,27</sup>. A basic linear SDE can be  
429 written as

$$430 \quad dX = -\alpha_X (X - \mu_X) dt + \sigma_X dB_t^{(X)} \quad (5)$$

431 This describes a mean-reverting Ornstein-Uhlenbeck process (OUP)  $X$ , which contains a  
432 systematic part (the  $dt$  term) and a stochastic part (the  $dB$  term). If the systematic part is  
433 dropped ( $\alpha_X = 0$ ), then equation (5) describes a Wiener process (WP, or random walk). The

434 OUP has expectation  $\mu_X$ , stationary standard deviation  $s_X = \sigma_X / \sqrt{2\alpha_X}$  and half-life

435  $t_{1/2,X} = \log(2) / \alpha_X$ . To model a hidden process, we can write

$$\begin{aligned}
 436 \quad dY_1 &= -\alpha_{Y_1}(Y_1 - Y_2)dt + \sigma_{Y_1}dB_t^{(Y_1)} \\
 dY_2 &= -\alpha_{Y_2}(Y_2 - \mu_Y)dt + \sigma_{Y_2}dB_t^{(Y_2)}
 \end{aligned} \tag{6}$$

437 Here, the measured process  $Y_1$  has a hidden process (or layer)  $Y_2$  folded into its systematic  
 438 part, such that  $Y_1$  tracks  $Y_2$ .  $Y_1$  is similar to an OUP, but instead of fluctuating around a fixed  
 439 expected value it fluctuates with a lagged response to the OUP  $Y_2$ .

440 When modelling connections between processes, we use vector notation. A pure  
 441 correlation between  $X$  and  $Y$  entails that the covariance matrix in front of the stochastic term  
 442  $d\mathbf{B}$  will have off-diagonal elements. If there is a causal connection from  $Y_2$  to  $X$ , for  
 443 instance, the system takes the following form

444  
 445

$$\begin{aligned}
 dX &= -\alpha_X(X - \mu_X - \beta_{Y_2 \rightarrow X}(Y_2 - \mu_X))dt + \sigma_X dB_t^{(X)} \\
 446 \quad dY_1 &= -\alpha_{Y_1}(Y_1 - Y_2)dt + \sigma_{Y_1} dB_t^{(Y_1)} \\
 dY_2 &= -\alpha_{Y_2}(Y_2 - \mu_Y)dt + \sigma_{Y_2} dB_t^{(Y_2)}
 \end{aligned} \tag{7}$$

447 where  $\beta_{Y_2 \rightarrow X}$  describes the connection strength from  $Y_2$  to  $X$ . Equation (7) describes a  
 448 “common cause” situation, where  $Y_2$  drives both  $X$  and  $Y_1$ .

449 To analyse the SCOR and DOT records, we first characterized each time series  
 450 separately, examining models with up to three layers (two hidden). In each model, the layers  
 451 could be WP or OUP (including fully deterministic layers where  $\sigma_i = 0$ ), excluding a one-  
 452 layered WP, which prohibits incoming causal links. We also excluded internal feedback  
 453 loops in multi-layer models because of numerical intractability. For both time series,  $\mu$  was  
 454 assigned a prior distribution  $\mu_i \sim N(0,1)$ , where  $i$  denotes the layer. All model parameters

455 were assigned normal priors, with 95 % prior probability ranges of  $\sigma_i \in (0.01, 1.0)$  for the  
456 stochastic term,  $t_{1/2,i} \in (0.1My, 50My)$  for the half life,  $\beta \in (-2, 2)$  for the causal connections,  
457 and  $\rho \in (-0.96, 0.96)$ , for the logit-transformed correlation coefficients. We used MCMC  
458 importance sampling to estimate Bayesian model likelihoods and calculate model  
459 probabilities.

460 The best model for SCOR in isolation was a one-layered OUP, while a three-layered  
461 model with a WP as the bottom driver was the best model for DOT in isolation. We then  
462 investigated all 15 connection models between these two best models, including the null  
463 hypothesis of no relationship (Supplementary Fig. 4). We allowed for causality from SCOR  
464 to DOT because both proxy records ultimately derive from deep-sea carbonate sediments,  
465 hence SCOR could in principle contain a signal of processes that have influenced DOT. The  
466 null hypothesis was assigned 50 % prior probability, while 50 % was distributed evenly  
467 among the 14 connection models. For model comparison, we used Jeffreys's scale to assess  
468 the strength of evidence represented by the Bayes factor  $B$ , where  $1 < B < \sqrt{10}$  is evidence  
469 "barely worth mentioning",  $\sqrt{10} < B < 10$  is "substantial evidence",  $10 < B < 10^{3/2}$  is  
470 "strong" evidence and  $B > 10^{3/2}$  is "very strong" evidence<sup>50</sup>.

471 The posterior probability of the null hypothesis was 11.2 % (Model 1; Supplementary  
472 Fig. 4), hence the Bayes factor favouring a connection between SCOR and DOT is 7.9  
473 (substantial evidence). The most probable model (Model 5; Supplementary Fig. 4) involves a  
474 feedback loop, where the upper DOT process (DOT1) affects SCOR positively while SCOR  
475 affects DOT1 negatively. All parameter estimates with credible intervals for the best model  
476 are presented in Supplementary Table 1. In the second most (and almost equally) probable  
477 model, (Model 12; Supplementary Fig. 4), SCOR affects the second DOT layer (DOT2)  
478 instead.

479           With a half-life of  $\sim 0.5$  Myr, SCOR responds to DOT processes on time scales  
480 comparable to those inferred from the other analyses (Fig. 3b, c). In contrast, DOT processes  
481 react very slowly to changes in SCOR (Supplementary Table 1), and because SCOR changes  
482 rapidly, the response in DOT will be smoothed out. From equation 5, the effect of SCOR on  
483 DOT1 is  $0.07 \text{ Myr}^{-1}$ , while the effect of DOT1 on the SCOR process is  $0.6 \text{ Myr}^{-1}$ . Thus, DOT  
484 influences SCOR much more strongly per time unit than vice versa.

485           The third most likely model (Model 4; Supplementary Fig. 4) only had a causal  
486 connection from DOT1 to SCOR, consistent with CCM and IT inferences. This model had a  
487 posterior probability of 17.5 %, hence the evidence for a feedback loop is less than  
488 “substantial” ( $B = 2.6$ ). In summary, we find evidence for there being at least one connection  
489 ( $B = 7.9$ ); for the connections to be causal rather than correlative given that there are  
490 connections ( $B = 12.5$ ); and specifically for a causal connection from DOT to SCOR given  
491 that there are connections ( $B = 15.4$ ).

492           We then repeated the analysis on untransformed data (not detrended or normalized),  
493 denoted uDOT and uSCOR. In this case, the best isolated model for both time series is a  
494 three-layer model with a WP at the bottom. The Bayes factor favouring a connection over no  
495 connection is 73, which is deemed “very strong evidence”. The best connection model  
496 involves a feedback loop between the top layers uDOT1 and uSCOR1. However, there is a  
497 very high probability for parameters enforcing cyclical behaviour, with a period of 1.5 Myr,  
498 which is consistent with an internal feedback loop model as the best isolated model for  
499 uDOT. Parameter estimates are shown in Supplementary Table 2.

500

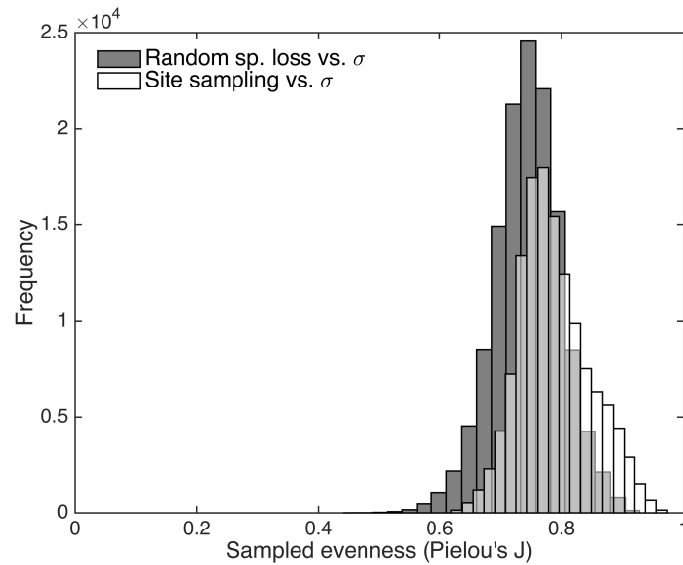
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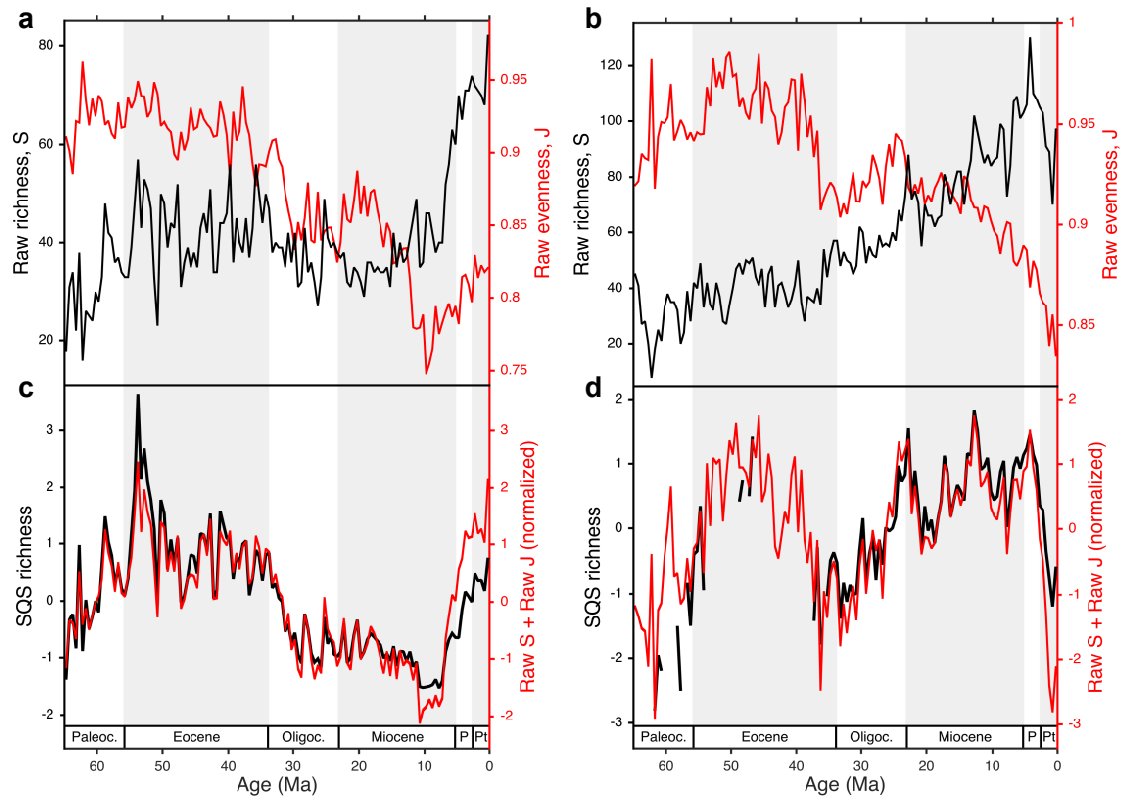
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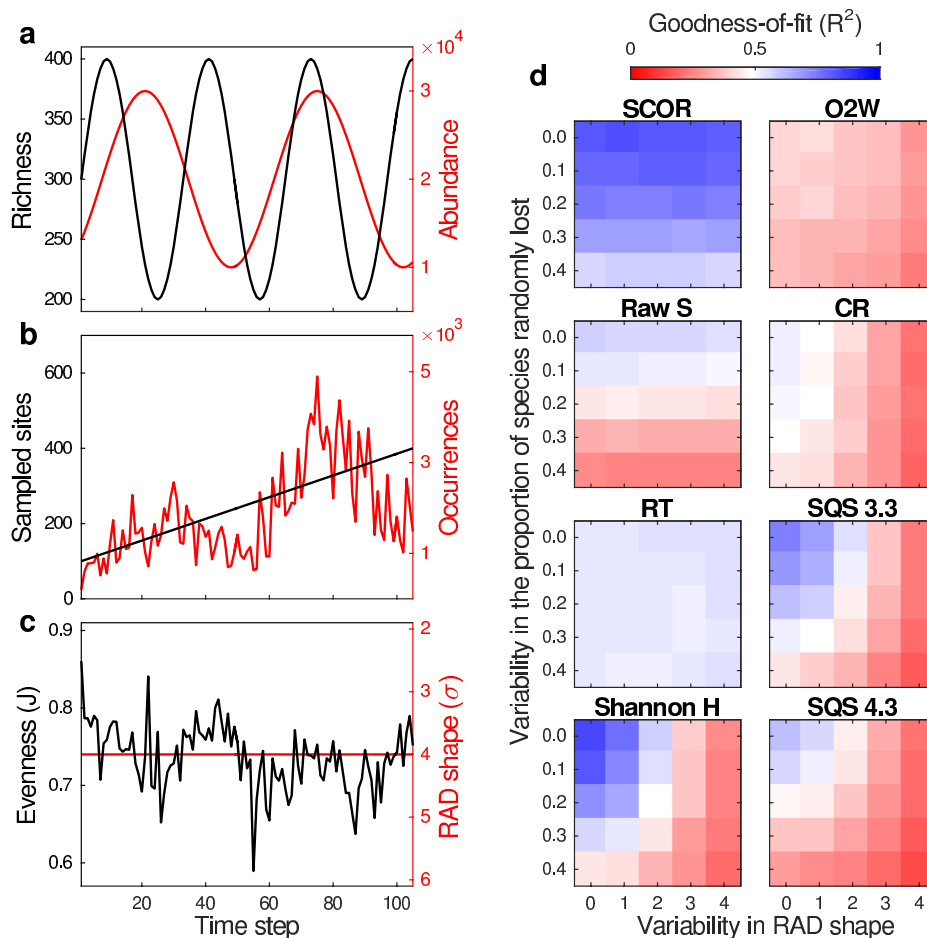
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**Supplementary Figure 1 | Distribution of sampled evenness across all Poseidon experiments.** Shaded histogram represents the model runs testing the sensitivity to variability in the proportion of species randomly removed, and variability in RAD shape parameter  $\sigma$  (Supplementary Fig. 3). Un-shaded histogram (note transparency in overlap) represents the model runs testing the sensitivity to variability in the proportion of sites sampled, and variability in  $\sigma$  (Fig. 1). The median evenness is 0.76, and 95 % of the values are in the range 0.65 - 0.90.

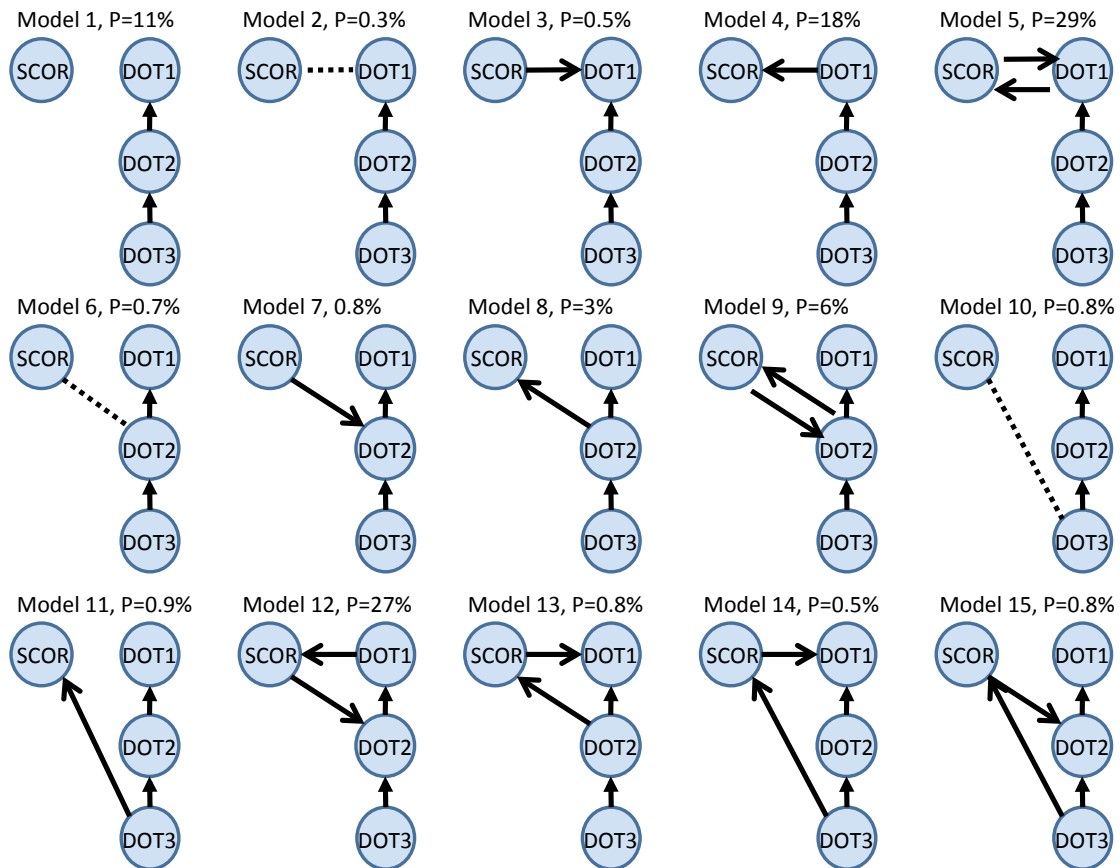


**Supplementary Figure 2 | Sampling-standardized richness can be reproduced by the sum of raw richness and evenness. a,b**, Raw sampled richness (S) and evenness (Pielou's J) of Cenozoic coccolithophores (a) and planktonic foraminifera (b) species from the NSB database. **c, d**, The sum of raw S and raw J superimposed on shareholder quorum subsampling (SQS) estimates of richness for coccolithophores (c) and foraminifera (d), all normalized to zero mean and unit standard deviation. SQS was calculated with a quorum level of 0.4 (higher quorum levels give nearly identical results but are less complete for the older part of the record). Ma, million years before present; Paleoc., Paleocene; Oligoc., Oligocene; P, Pliocene; Pt, Pleistocene.



### Supplementary Figure 3 | Effect of random species loss in Poseidon model

**experiments. a**, Simulated richness and abundance as in Fig. 1a. **b**, Site sampling increases smoothly in all experiments. Instead, a proportion of the species is randomly removed in each time step, causing volatility in occurrences. No variability in the proportion lost means that 50 % are always removed. In this example, variability = 0.4, meaning that between 30 % and 70 % of species are lost. **c**, Even with a constant original RAD shape, random species loss, and variability in the proportion lost, generates volatility in sampled evenness (this example is an extreme case, see Supplementary Fig. 1). **d**, Sensitivity to variability in RAD shape and in the proportion of species lost. Values are median goodness-of-fit ( $R^2$ ) of 50 model runs, comparing SCOR to true abundance, and richness estimates to true richness.



#### Supplementary Figure 4 | Schematic of all connection models between SCOR

and DOT in linear SDE analysis. The best model for SCOR in isolation is a one-layered OUP. The best model for DOT in isolation is a three-layered model with a WP as the bottom layer (DOT3). All models possible between these two best models are shown. Note that SCOR cannot drive DOT3 because DOT3 is a WP. Percentage values represent posterior model probabilities. Solid arrows represent casual connections pointing from driver to response. Dotted lines represent correlative relationships. See Methods for details.

**Supplementary Table 1 | Parameter estimates for the most probable connection model between SCOR and DOT**

Parameter	Estimate (posterior median)	95 % credible interval
$t_{1/2,SCOR1}$	0.53 Myr	(0.33, 1.1) Myr
$s_{SCOR1}$	0.94	(0.65, 1.1)
$\mu_{SCOR}$	0.43	(-0.01, 0.94)
$t_{1/2,DOT1}$	8.0 Myr	(0.91, 31) Myr
$s_{DOT1}$	1.2	(0.37, 2.4)
$t_{1/2,SDOT2}$	16 Myr	(3.4, 166) Myr
$s_{DOT2}$	0.45	(0.03, 2.8)
$\sigma_{DOT3}$	0.027	(0.003, 0.22)
$\beta_{DOT1 \rightarrow SCOR1}$	0.45	(0.14, 0.76)
$\beta_{SCOR1 \rightarrow DOT1}$	-0.77	(-2.3, 0.5)

Parameter estimates for Model 5 (Supplementary Fig. 4), where  $t_{1/2,i}$  are half-lives,  $s_i$  are the stationary standard deviations,  $\mu_i$  are the expected values of OUP,  $\sigma_i$  are stochastic terms in WP. The bottom DOT layer (DOT3) is a WP. The interpretation of parameter values depend on other processes, e.g. the causal connection from DOT to SCOR will increase the total stationary standard deviation of the SCOR process. The reported  $s_i$  values represent what the process itself supplies in isolation. See Methods for details.

**Supplementary Table 2 | Parameter estimates for the most probable connection model between uSCOR and uDOT**

<b>Parameter</b>	<b>Estimate (posterior median)</b>	<b>95 % credible interval</b>
$t_{1/2,uSCOR1}$	0.91 Myr	(0.32, 1.6) Myr
$S_{uSCOR1}$	0.07	(0.01,0.35)
$t_{1/2,uSCOR2}$	2.4 Myr	(0.86, 68) Myr
$S_{uSCOR2}$	0.7	(0.02,21)
$\sigma_{uSCOR3}$	2.8	(0.04, 5.8)
$t_{1/2,uDOT1}$	0.24 Myr	(0.13, 0.33) Myr
$t_{1/2,uDOT2}$	0.50 Myr	(0.21, 1.5) Myr
$\sigma_{uDOT3}$	4.1	(1.9, 8.9)
$\beta_{uDOT1 \rightarrow uSCOR1}$	2.7	(-2.6, 3.8)
$\beta_{uSCOR1 \rightarrow uDOT1}$	-2.7	(-5.2, 1.9)

Symbols and interpretations as in Supplementary Table 1, but in this case both uDOT and uSCOR have 3-layer models with a WP at the bottom. See Methods for details.