

RESEARCH

Evolution of Hierarchy in Bacterial Metabolic Networks

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Abstract

Background: In self-organized systems, the concept of flow hierarchy is a useful way to characterize the movement of information throughout a network.

Hierarchical network organizations are shown to arise when there is a cost of maintaining links in the network. A similar constraint exists in metabolic networks, where costs come from reduced efficiency of nonspecific enzymes or from producing unnecessary enzymes. Previous analyses of bacterial metabolic networks have been used to predict the minimal nutrients that a bacterium needs to grow, its mutualistic relationships with other bacteria, and its major ecological niche. Using flow hierarchy, we can also infer the tradeoffs between growth rate and metabolic efficiency that bacteria make given their environmental constraints.

Results: Using a comparative approach on 2,935 bacterial metabolic networks, we show that flow hierarchy in bacterial metabolic networks tracks a fundamental tradeoff between growth rate and biomass production, and reflects a bacterium's realized ecological strategy. Additionally, by inferring the ancestral metabolic networks, we find that hierarchy decreases with distance from the root of the tree, suggesting the important pressure of increased growth rate relative to efficiency in the face of competition.

Conclusions: Just as hierarchical character is an important structural property in efficiently engineered systems, it also evolves in self-organized bacterial metabolic networks, reflects the life-history strategies of those bacteria, and plays an important role in network organization and efficiency.

Keywords: modularity; hierarchy; metabolism; bacteria; reverse ecology

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2

3 Background

4 In characterizing bacteria, we seek to understand both their internal processes and
5 how they interact with other species and their environments. Techniques in cell and
6 molecular biology have been very helpful in revealing the inner workings of bacte-
7 ria, but do not address the ecological context in which bacteria develop and live.
8 Increasingly, metagenomic techniques are being used to simultaneously sequence all
9 of the bacteria present in a given environment. However, these techniques can only
10 provide limited information about particular species, where they are found, their
11 relative abundances, and co-occurrence patterns.

12 By studying the structure and evolution of a bacterium's metabolic network, we
13 can move beyond correlational profiles to understand both the underlying pressures
14 that have driven its evolution as well as the ecological role it occupies. A bacterium's
15 ability to reproduce depends on the efficiency of its metabolism, which we can
16 study as a network of metabolites linked together by the enzymes that transform
17 one metabolite into another [1]. The structure of these networks varies across the
18 bacterial kingdom and reflects the environmental pressures that guide bacterial
19 evolution. Thus, a bacterium's metabolic network can be used to predict the minimal
20 nutrients that it needs to grow, its mutualistic relationships with other bacteria, and
21 its major ecological niche [2][3][4]. In describing metabolic networks, two types of
22 hierarchies can be helpful: flow hierarchy and containment hierarchy.

23 Previous study of the hierarchical nature of metabolic networks has tended to
24 focus on containment hierarchy, which represents the nodes in a network as being
25 contained within modules, which themselves are contained within other modules,
26 and so on, in a recursive fashion. For example, a containment hierarchy may be used
27 to represent the organization of a firm, with divisions, departments, teams and in-
28 dividual employees. Applied to metabolic networks, such modules correspond to
29 known pathways [11][12], and modular hierarchy has been hypothesized to increase
30 evolvability of metabolism [13]. Simulations of Boolean logic networks have sug-
31 gested that modularity evolves in changing environments, and it has been hypothe-
32 sized that this would be reflected in bacterial metabolic networks[14][15]. However
33 this has not been borne out [16]; differences in modularity of metabolic networks
34 have been found to be moderately correlated with the phylogenetic divergence of

35 the organisms, and there is a general trend of loss of modularity over evolutionary
36 time due to the addition of peripheral pathways during niche specialization [17].

37 In this work, we focus on the heretofore neglected type of hierarchy: flow hierarchy.
38 While containment hierarchy represents the organization of a network as a series
39 of modules, flow hierarchy characterizes the way information moves throughout the
40 network. Information is acquired at the lowest level of the hierarchy and transmitted
41 to higher levels, where it is aggregated and passed upward; at the same time orders
42 come from the top of the hierarchical network and are passed down to lower levels.

43 Flow hierarchy is used to describe networks in many fields, particularly in the
44 study of information accrual networks. In engineering, information accrual networks
45 are used in the design of control systems, and in the social sciences, they are used to
46 study the organization of firms [5][6]. To use the example of the firm, flow hierarchy
47 could be used to represent the movement of orders and responsibilities throughout
48 the firm, as low-level employees report upwards to supervisors who aggregate reports
49 for department heads and so on, while orders flow downward from decision makers
50 to executors. As bacteria synthesize the complex molecules needed for survival, they
51 reduce the overall entropy within the cell. Given the thermodynamic equivalence of
52 entropy reduction and information accrual, this reduction can also be viewed as an
53 increase of information. Thus we can use the metabolic network graph to study the
54 flow of information through the cell.

55 Although flow hierarchy (hereafter referred to as hierarchy) has not been well stud-
56 ied in metabolic networks, it has been identified in a variety of other self-organized
57 networks, including food webs, neural networks, and the transcription factor net-
58 work in *D. melanogaster*, where the degrees of hierarchy were significantly higher
59 than would be expected in a random network with the same degree distribution [7].
60 In studying hierarchy in metabolic networks, we are able not only to learn that
61 hierarchy appears higher than would be expected by a random configuration, but
62 also to assess adaptive benefits that hierarchy provides.

63 These findings show that hierarchy is common among self-organized networks,
64 but they do not explain when hierarchical network organization would provide a
65 selective advantage. A number of comparative approaches have been used to make
66 inferences about the forces guiding the development of networks in other disci-
67 plines, and from them we can deduce some of the adaptive benefits that hierarchy

68 provides. Simulated evolution experiments of Boolean logic networks have shown
69 that the cost of maintaining links between nodes is the driving force in the emer-
70 gence of hierarchy [19]. Hierarchical characteristics have also been shown to predict
71 the costs of maintaining information-sharing relationships in emergent social net-
72 works and reflect the degree of market variability that supply chains may be able to
73 withstand [21]. We know that bacterial metabolic networks face similar constraints.
74 Maintaining catalytic abilities between metabolites incurs a cost either as a trade-
75 off between specificity and efficiency, or from production and replication of unused
76 enzymes [20][22]. We show that the strength of these constraints is correlated with
77 degree of hierarchy in metabolic networks.

78 To measure flow hierarchy quantitatively, researchers commonly use the global
79 reaching centrality (GRC), defined as the average difference between the maximum
80 local reaching centrality (i.e. fraction of nodes in the network accessible by each node
81 of the network) and the local reaching centrality [23]. In essence, GRC is a measure
82 of heterogeneity in the flow of information throughout a network. For example, a
83 dictatorial firm where the boss exerts great influence over the entire company while
84 individual employees have little sway would have a higher GRC than a consulting
85 firm run by a group of partners, each of whom oversees a small group of highly
86 collaborative employees. Other, less widely used measures of flow hierarchy are an
87 eigenvector centrality based method, the fraction of edges participating in cycles,
88 or by decomposition into treeness, feedforwardness, and orderability [7][8][9].

89 Studying the evolution of containment hierarchy can tell us about the environ-
90 mental contingencies that inform the evolution of metabolic networks (e.g. resource
91 availability, temperature, environmental variation, etc). However, by studying flow
92 hierarchy we can also infer the different growth strategies a bacterium may pursue,
93 furthering our understanding of how it fills its ecological niche [13]. We employ
94 the reverse ecology principle to understand how the hierarchical character of a
95 metabolic network reflects the life-history strategy of a bacterium in relationship to
96 the growth-yield tradeoff, as well as its environmental niche. As bacteria first adapt
97 to new habitats they may develop novel metabolic functions, leading to an increase
98 in hierarchy, since the new metabolic functions are added to the periphery of the
99 network.

100 As those ecosystems evolve, however, some bacteria may adopt higher-growth
101 rate strategies in response to increased competition, at the expense of efficiency
102 and consequently metabolic network hierarchy. Since only some bacteria adopt such
103 high-growth rate strategies, while others maintain higher degrees of hierarchy and
104 efficiency, variance in hierarchy increases overall. Though both hierarchy and mod-
105 ularity correlate with bacterial specialization, we find that, contrary to the Boolean
106 network simulations, there is little evolutionary relationship between the two, and
107 that there is more conservation of hierarchy than modularity over time.

108

109 **Results and Discussion**

110 **Networks**

111 Networks were reconstructed from 2,935 bacteria species in the KEGG database.
112 These networks were robust to misannotation of enzymes. In random perturbations
113 of the metabolic network for *E. coli* with 10% of the reactions removed, 95% the
114 networks had hierarchy scores within 12% of the true network, and with 10% of
115 reactions reversed, within 6% of the true network.

116 Network sizes ranged from 76 to 1496 metabolites, with a mean of 848. The
117 smallest was the obligate insect parasite *Nasuia deltocephalinicola* and the largest
118 was the soil bacterium *Burkholderia lata*.

119 **Hierarchy**

120 Hierarchy scores for the metabolic networks were calculated using the GRC hierar-
121 chy score [23]. The mean degree of hierarchy was 0.279, and ranged from 0.065, for
122 the insect symbiote Candidatus *Nasuia deltocephalinicola*, to 0.385 for a *Blattabac-*
123 *terium* endosymbiont of *Nauphoeta cinerea*, an insect endosymbiote. The hierarchy
124 score for *E. coli* strains was 0.269 (Figure 1). For comparison with a random net-
125 work and real world networks, GRC hierarchy scores for an Erdős-Rényi random
126 graph is 0.058, a scale-free network 0.127, and a tree 0.997, an estuary food web
127 0.814, and the neuronal network of *C. elegans* [23].

128 **Relationship to environment and growth rate**

129 There is a fundamental ecological trade off between growth rate and yield, which is a
130 result of the underlying efficiencies of the reactions. Bacteria that have a metabolism

131 that produces the maximal growth rate per amount of carbon taken up will have
132 suboptimal biomass production, and vice versa.

133 This tradeoff is representative of fundamentally divergent ecological strategies that
134 bacteria use [24]. Furthermore, the tradeoffs between growth and yield are repre-
135 sented in the constraints on the metabolic network, such that high-yield strategies
136 lead to more hierarchical networks. There is a tradeoff between enzyme specificity
137 and efficiency, so when yield is favored there will be higher costs of maintaining
138 edges in the network, which leads to hierarchy [25] [20]. Rapidly growing bacte-
139 ria have more metabolic cycles which allow for metabolic flexibility at the cost of
140 wasted energy, and these cycles decrease hierarchy [26]. The cost of maintaining
141 unused enzymes in the genome is higher when efficiency is paramount [22].

142 Using a dataset of 111 bacteria with known growth rates, we see that the hier-
143 archical character of the network correlates inversely with growth rate, Spearman
144 $\rho = -0.31$, $p < 0.0007$, fig 2. Furthermore, there is evidence that carbon efficiency
145 constraints on bacteria differs greatly by environment, and that the evolutionary dy-
146 namics of carbon usage niche specialization are stronger within populations [27][28].
147 When we control for the bacterial environment, we see a correlation of $\rho = -0.41$,
148 which is significantly greater than 0 ($p < 0.0001$, and significantly greater than the
149 correlation when not controlling for the environment $p < 0.003$). Bacteria with hier-
150 archy score greater than the median hierarchy score grow at a rate of 0.64 doublings
151 per hour, compared to 1.44 doublings per hour for bacteria with hierarchy score less
152 than the median, *i.e.* bacteria with the less hierarchical metabolic networks grow
153 2.25 times faster than those with more hierarchical networks ($p < 0.0002$).

154 Thus the hierarchical character of the metabolic networks reflects the growth
155 rate of the organisms and their environmental niche. These constraints of edge
156 weight and tradeoffs between hierachical and ahierachical networks in metabolism
157 are similar to those made in social networks and supply chains [20] [21].

158 Relationship to other network properties

159 In addition to measuring hierarchy, we evaluated a number of other network statis-
160 tics. We computed node count, edge count, modularity (as evaluated by the Girvan-
161 Newman algorithm [29]), clustering coefficient, full diameter, effective diameter,
162 number of strongly connected components, proportion of the nodes in the largest

163 strongly connected component, and Luo Hierarchy score, an alternative metric of
164 hierarchy that measures the proportion of edges that do not participate in any cy-
165 cles. Edge and node count correlated most strongly with genetic distance. However,
166 after these basic structural properties, the statistics that correlated most highly
167 with genetic distance were the Girvan-Newman modularity score and the GRC hi-
168 erarchy score (Table 1). We also computed the partial correlation for each variable
169 with genetic distance, controlling for the others, and found that the GRC metric
170 had the highest partial correlation.

171 Hierarchy Over Time

172 The hierarchy of the KEGG bacteria and reconstructed ancestors seems to first
173 increase, and then decrease with distance from the root of the tree (Figure 3).
174 Interestingly, with the dataset of 2,935 from the latest KEGG database, the cor-
175 relation of modularity and distance from the root of the tree found by Kreimer *et*
176 *al.* [17] is actually reversed. Modularity appears to increase rather than decrease
177 with distance from the root, (Figure 4). This correlation remains positive when
178 restricting analysis to the species used by Kreimer *et al.*.

179 As bacteria specialize to niches in a given ecosystem, they take on different
180 metabolic strategies, which are reflected in the hierarchical profile of the metabolic
181 network. This difference in strategies is consistent with the rise and fall of hierarchy
182 over the evolutionary trajectory. As microbes first adapt to new environments or
183 habitats (niche *sensu* Grinnell) they must gain novel metabolic functions, which are
184 added as pathways in the periphery in the network and which increases the hier-
185 archical character [30]. As complex relationships develop within the habitats, and
186 bacteria adapt to different resource use profiles and competitive strategies (niche
187 *sensu* Elton), the hierarchical profile of the metabolic network diversifies. Thus, the
188 decrease in hierarchy over evolutionary time is caused by more bacteria specializing
189 in a rapid-growth strategy, but the increasing variance in hierarchy reflects the fact
190 that not all bacteria adopt this strategy. In studying the adaptive strategies chosen
191 by different bacteria, we may be able to make inferences about the bacteria and
192 their environments, as well as the interplay between evolutionary and ecological
193 dynamics.

194 Correlation of Modularity and Hierarchy

195 Hierarchy and modularity are global properties of metabolic networks. Both cor-
196 relate with bacterial specialization and both change with distance from the root
197 of the phylogenetic tree. Using the method of phylogenetic independent contrasts
198 to look for correlation independent of phylogenetic structure, we found a mod-
199 erate inverse correlation between modularity and hierarchy (Pearson correlation
200 $r = -0.18, p < 10^{-15}$), suggesting little evolutionary relationship between modu-
201 larity and hierarchy [31]. Interestingly, simulated Boolean networks demonstrate a
202 positive correlation between modularity and hierarchy [19].

203 Conclusion

204 Characterizing the hierarchical structure of metabolic networks is useful in un-
205 derstanding the constraints under which these networks evolve. Hierarchy corre-
206 lates with phylogenetic divergence, as would be expected for a trait subject to
207 natural selection. This correlation is similar to the correlation of phylogenetic dis-
208 tance and modularity, suggesting that the hierarchical organization of networks,
209 like modular organization, is important for function. However, modularity should
210 be viewed as complementary to, rather than supplanted by, hierarchy when analyz-
211 ing the global organization of metabolic networks. Both structural properties are
212 conserved across phylogenies and evolve together. A better understanding of the
213 character of metabolic networks is valuable in the growing field of ‘reverse ecol-
214 ogy,’ in which the observed networks can be used to make inferences on possible
215 environments [2][32][33].

216 By algorithmically reconstructing the metabolic networks, we are able to perform
217 a larger-scale analysis than has previously been reported. Although the reaction
218 annotations in KEGG may be prone to errors or omissions, we find that the GRC
219 hierarchy metric is robust to small amounts of reaction omissions or reversals. By
220 expanding the scope of the analysis, we find that modularity is actually inversely
221 correlated with distance from the root of the tree, contrary to what has been found
222 in previous studies of a more limited set of bacteria.

223 From reconstructed ancestral metabolic networks, we are able to infer how hierar-
224 chy evolves in networks over time, and understand the interplay between evolution-
225 ary and ecological dynamics. Hierarchy shows an increase followed by a decrease

226 across the phylogenetic tree, which is reflective of the adaptive process of bacteria,
227 first to novel fundamental niches, and then to a realized niche. The net trend in
228 decreasing hierarchy reflects a dominance of fast-growth, low-efficiency strategy.

229 **Methods**

230 Hierarchy Metric

231 Hierarchy scores were calculated using the global reaching centrality metric devel-
232 oped by Mones *et al.*, which is based on the local reaching centrality [23]. The
233 local reaching centrality (LRC) of a node in a network is the fraction of the nodes
234 of the network that can be reached starting at the focal node. More precisely, if
235 the metabolic network is represented as a graph, $G = (V, E)$ it can be said that v
236 reaches v' if there exists a series of edges $(v, v_i), (v_i, v_j) \dots (v_j, v') \in E$. Let $R(v)$ be
237 the set of nodes $v' \in V$ where v' is reachable from v . Then the LRC of v is $\frac{|R(v)|-1}{|V|-1}$.
238 The GRC is then $\frac{1}{|V|-1} \sum_{v \in V} \max_{v' \in V} \text{LRC}(v') - \text{LRC}(v)$

239 Modularity Metric

240 The modularity metric was calculated using the SNAP package [34]. The modularity
241 of a network is the optimal partitioning of the nodes into clusters to maximize
242 $Q = \frac{1}{4m} \sum_{ij} \left(A_{ij} - \frac{k_i k_j}{2m} I_{ij} \right)$. Where m is the number of edges in the network, A_{ij}
243 is the adjacency matrix, i.e. A_{ij} is 1 if there is an enzyme that converts metabolite
244 i into metabolite j . k_i is the number of reactions that metabolite i participates in,
245 and $I_{ij} = 1$ if i and j are in the same module, and -1 otherwise. Since finding the
246 global optimal of Q is an NP-hard problem, we use the method developed by Girvan
247 and Newman, which partitions the network by iteratively removing the edge with
248 the highest betweenness centrality [29].

249 Robustness of Reconstruction

250 The KEGG database is large, with heavy manual curation; however, this does not
251 mean that the data are always perfect. A reaction may be favorable in one direction
252 in a model organism in laboratory conditions, but might proceed in the opposite
253 direction or become bidirectional in different environments or species. It is also
254 possible that reactions are missing from the database, or that an enzyme placed
255 in an orthology group based on the study of one species may catalyze a different
256 reaction in other species. To evaluate robustness to errors in the KEGG database,

257 we examined the network for the well-studied bacterium, *E. coli*. We performed 100
258 replicates dropping or reversing 10% of the reactions, evaluated the hierarchy scores
259 of these networks, and calculated the spread of the central 95% of hierarchy scores.

260 Reconstruction of Genetic Distance

261 Following the methods often used in bacterial comparative genomics [35][3][36], for
262 each of the 2,935 species, the 16s ribosomal sequence from KEGG was aligned to
263 the Greenegenes database using PyNast, resulting in multiple sequence alignments
264 for the 2,935 species [37][38]. The genetic distances between all pairs of bacterial
265 species were computed using the Kimura distance metric [39].

266 Reconstruction of Networks

267 For each bacterial species, a network of metabolites was inferred based on the en-
268 zymes present in the genome, the reactions known to be catalyzed by the enzymes
269 present or orthologous enzymes, and a database of reaction substrates and prod-
270 ucts. The KEGG database of the genomic content of the 2,935 bacterial genomes
271 was used to identify which enzyme classes were present in each genome and which re-
272 actions were present [40]. The reaction information from KEGG was supplemented
273 by a the bioreaction database from Stelzer *et al.* which excludes currency metabo-
274 lites, improves on predictions of directionality of reactions, and, for reactions with
275 multiple substrates and products, provides carbon tracking of which substrates are
276 converted to which products [41]. Using this reaction information, networks were
277 constructed with metabolites as nodes, and a directed edge was placed between
278 metabolites if there was a reaction that converted one metabolite to another. If re-
279 actions were reversible, then bi-directional edges were added between the substrates
280 and products.

281 Ancestral Networks

282 To construct the ancestral networks, a phylogenetic tree was reconstructed using
283 RAxML 8.2.9 and the 16-state GTR nucleotide substitution model with gamma
284 rate heterogeneity [42]. The branch-length weighted average bootstrap support of
285 the partitions over 300 trees was 85.4. Using the maximum likelihood estimate of the
286 best tree, at each interior node of the phylogenetic tree, a genome was constructed
287 using the Fitch small parsimony algorithm. In cases where the presence or absence

288 of a gene was equally parsimonious, the gene was randomly selected to be included.
289 These ancestral genomes were then used to reconstruct ancestral networks, just as
290 the networks were constructed on the leaves of the tree.

291 Niche strategies

292 Growth rate data for 113 bacterial species and environmental annotations for those
293 bacteria, which for 68 species were gathered from NCBI, and manual curation fol-
294 lowing literature review was used for the remaining 45 [43][4]. Due to their low
295 number, the two aquatic species in the data set were excluded from further anal-
296 ysis. Correlations were calculated as Spearman's ρ . To calculate correlation con-
297 trolling for environment, ρ was calculated within each environment, and a species
298 weighted-average across environments was computed. Due to several bacteria hav-
299 ing the same growth rates, p -values were calculated using permutation tests rather
300 than the Student's t -distribution approximation. Significance tests were performed
301 with 100,000 permutations each. For the overall ρ , permutations were done across
302 all bacteria. To test the strength of the habitat-controlled correlation, growth rates
303 were permuted within habitat classes and the species-weighted ρ was computed for
304 each permutation. To test the effect of controlling for the environment, habitat la-
305 bels were permuted and the difference between the species weighted ρ and overall
306 ρ was computed.

307 Consent to Publish

308 All authors have approved this manuscript for submission. This work has not been published or submitted elsewhere.

309 Competing interests

310 The authors declare that they have no competing interests.

311 Author Contributions

312 AG designed the experiment, carried out the analysis, and wrote the paper. MF provided critical guidance on the
313 direction of the work, and revision of the manuscript.

314 Availability of the Data

315 The dataset supporting the conclusions of this article, specifically the reconstructed metabolic network
316 (Supplementary File 1) and topological statistics (Supplementary File 2) of these networks, are included within the
317 article (and its additional files).

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	Correlation	Partial Correlation
Node Count	0.26***	0.03***
Edge Count	0.27***	-0.02*
Modularity	0.28***	0.05***
GRC Hierarchy	0.28***	0.17***
Luo Hierarchy	0.22***	-0.06***
Largest SCC Fraction	0.30***	0.12***
Cluster Coefficient	0.13***	0.03***
Full Diameter	0.23***	0.06***
Effective Diameter	0.20***	0.01
SCC Count	0.14***	0.02**
Mean Degree	0.24***	-0.04***

Table 1 Correlation of network statistics with phylogenetic distances, and partial correlation of network statistic with phylogenetic distance, controlling for the other variables. The correlation and partial correlation of GRC Hierarchy metric with genetic distance is higher than all other non-trivial metrics. ***: p value < 0.001, **: p value < 0.01, *: p value < 0.05.

424 **List of Figures**

425 1 Histogram of GRC hierarchy scores of the 2,935 bacteria in the
426 KEGG database. Mean degree of hierarchy is 0.279, ranging from
427 0.065 for the insect symbiote *Candidatus Nasuia deltocephalinicola*
428 to 0.385 for a *Blattabacterium* endosymbiont of *Nauphoeta cinerea*,
429 an insect endosymbiont. The hierarchy score for *E. coli* strains is 0.269. 17

430 2 The relationship between hierarchical character and growth rate re-
431 flects fundamental tradeoffs between growth and yield and is informa-
432 tive about the ecological niche the bacteria occupy. Overall, growth
433 rate is inversely correlated with hierarchy (Spearman's rank correla-
434 tion, $\rho = -0.31$, $p = 0.00065$). When controlling for bacterial envi-
435 ronment the trend becomes stronger ($\rho = -0.41$, $p = 0.0001$). The
436 outlier in the facultative parasite pane is *Borrelia burgdorferi*, which
437 is an obligate parasite that alternates between insect and vertebrate
438 hosts, and thus is similar to the obligate parasites. The particular
439 strain also lacks a number of enzymes in its glycolysis pathway that
440 are present in other *B. burgdorferi* strains that have hierarchy scores
441 of 0.183 ± 0.002 18

442 3 Hierarchy has a slight overall decrease with phylogenetic distance
443 (Spearman's rank correlation, $\rho = -0.06$, $p < 10^{-6}$). Hierarchy ap-
444 pears to increase and then decrease further from the root of the tree. 19

445 4 Modularity increases with phylogenetic distance (Spearman's rank
446 correlation, $\rho = 0.31$, $p < 10^{-15}$). 20







