

# 1 **Morphometrics reveals complex and heritable apple leaf shapes**

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8

## 9 **Abstract**

10

11 Apple (*Malus spp.*) is a widely grown and valuable fruit crop. Leaf shape and size are important  
12 for flowering in apple and may also be early indicators for other agriculturally valuable traits.

13 We examined 9,000 leaves from 869 unique apple accessions using linear measurements and  
14 comprehensive morphometric techniques. We identified allometric variation in the length-to-  
15 width aspect ratio between accessions and species of apple. The allometric variation was due to  
16 variation in the width of the leaf blade, not length. Aspect ratio was highly correlated with the  
17 primary axis of morphometric variation (PC1) quantified using elliptical Fourier descriptors  
18 (EFDs) and persistent homology (PH). While the primary source of variation was aspect ratio,  
19 subsequent PCs corresponded to complex shape variation not captured by linear measurements.

20 After linking the morphometric information with over 122,000 genome-wide SNPs, we found  
21 high narrow-sense heritability values even at later PCs, indicating that comprehensive  
22 morphometrics can capture complex, heritable phenotypes. Thus, techniques such as EFDs and  
23 PH are capturing heritable biological variation that would be missed using linear measurements

24 alone, and which could potentially be used to select for a hidden phenotype only detectable using  
25 comprehensive morphometrics.

26

## 27 **Introduction**

28

29 Apples (*Malus spp.*) are one of the world's most widely grown fruit crops, with the third highest  
30 global production quantity of over 84 million tonnes in 2014 (1). The shape and size of apple  
31 leaves plays an essential role in the growth and development of the tree, and ultimately impact  
32 characteristics of the fruit. Apple leaves are generally simple, with an elliptical-to-ovate shape.  
33 Previous studies in apple used linear measurements, such as length and width, to quantify leaf  
34 shape (2, 3). The length-to-width aspect ratio is a major source of variation in leaf shape.

35 Differing aspect ratios lead to a disproportionate increase or decrease in length relative to width,  
36 or allometric variation, in leaves (4, 5). While linear measurements such as leaf length and width  
37 are useful, they fail to capture the full extent of leaf shape diversity. Failing to measure leaf  
38 shape comprehensively also limits our ability to discern the total underlying genetic  
39 contributions.

40

41 Elliptical Fourier descriptors (EFDs) are a valuable, well-recognized tool for quantifying the  
42 outline of a shape. EFD analysis first converts a contour to a chaincode, a lossless data  
43 compression method that encodes shape by a chain of numbers, in which each number indicates  
44 step-by-step movements to reconstruct the pixels comprising the shape. A Fourier decomposition  
45 is subsequently applied to the chain code, quantifying the shape as a harmonic series. EFDs have  
46 been used extensively to quantify leaf shape in diverse species, such as grape (6), tomato (7), and

47 *Passiflora* (8). Previous work used EFDs to assess apple fruit shape (9), but this technique has  
48 not yet been applied to apple leaves. A newly developed morphometric technique, persistent  
49 homology (PH), provides another method for estimating leaf shape. PH, like EFDs, is  
50 normalized to differences in size, but it also could be orientation invariant. PH treats the pixels of  
51 a contour as a 2D point cloud before applying a neighbor density estimator to each pixel. A  
52 series of annulus kernels of increasing radii are used to isolate and smooth the contour densities.  
53 The number of connected components is recorded as a function of density for each annulus,  
54 resulting in a curve (a reduced version of persistent barcode) that quantifies shape as topology.  
55 The topology-based PH approach can also be applied to serrations and root architecture, allowing  
56 the similar framework to be used across different plant structures (10, 11).

57

58 Comprehensively measuring leaf shape, using approaches such as EFDs and PH, is important, as  
59 shape features may be associated with agriculturally important traits. Leaves are present during  
60 the lengthy juvenile phase in apple but fruits appear only on mature trees and thus, leaf traits can  
61 enable early selection without the need for genetic markers. In apple, it generally takes 5 years  
62 for significant fruiting to occur and any ability to discard trees not possessing a trait of interest  
63 earlier in development is extremely valuable (12). There are already several cases of unique leaf  
64 characteristics providing an early marker for other genetic differences in apple. For example, the  
65 gene underlying red fruit flesh color may lead to anthocyanin accumulation in the leaves, causing  
66 red foliage (13, 14) while columnar tree architecture may be accompanied by an increase in leaf  
67 number, area, weight per unit area and length-to-width ratio (15). Leaf pH has also been  
68 proposed as an early indicator of low acid fruit (16).

69

70 In addition to serving as early markers for other traits, leaf shape and size may influence the  
71 amount of light a tree receives, and light exposure is crucial for flowering in apple. Light  
72 penetration results in higher levels of flowering, while leaf injury or defoliation can reduce  
73 flowering (17). Thinning apple trees to a particular leaf-to-fruit ratio is a common practice to  
74 attain optimal fruit color and size. Contrastingly, trees with fewer fruit may increase vegetative  
75 growth and thus leaf area (18). In previous work, several leaf traits such as area and perimeter  
76 were correlated with apple fruit size (19). Clearly, there is an important relationship between the  
77 leaves and the fruit, and comprehensively quantifying the variation in leaf shape is a crucial  
78 component to understanding this relationship in apple.

79

80 Leaves are the main photosynthetic organs of apple, but the genetic basis underlying their shape  
81 and size remains unknown. In cotton, a single locus controls the major leaf shapes (20), but in  
82 most instances leaf shape appears to be controlled by numerous small-effect loci (5, 21). There  
83 are limited examples of genomic analyses of leaf shape in apple, however, a previous bi-parental  
84 linkage mapping study found two suggestive quantitative trait loci for leaf size (2). Previous  
85 work also measured several leaf traits such as area, perimeter and circularity, in 158 apple  
86 accessions. The study linked these measurements with 901 single nucleotide polymorphisms  
87 (SNPs) but found no significant genotype-phenotype relationships (19). Thus far, efforts have  
88 not been made to estimate the genetic heritability of comprehensive morphometric leaf  
89 phenotypes, such as those described using EFDs and PH. It therefore remains unclear to what  
90 extent these methods are capturing biologically meaningful, heritable variation.

91

92 To fully understand the genetic basis of leaf shape, it is essential to include both linear and  
93 morphometric estimates of shape. Decreasing sequencing costs and access to a large and diverse  
94 germplasm collection allowed us to analyze approximately 9,000 leaves from over 800 unique  
95 accessions which we linked to over 122,000 genome-wide SNPs. We present the first  
96 comprehensive analysis of leaf shape in apple, revealing that both accessions and species show  
97 allometric variation due to differences in the width of the leaf blade. While the primary axis of  
98 variation in apple using EFDs and PH is due to this allometric variation, we find high narrow-  
99 sense heritability values even at later principal components, indicating that comprehensive  
100 estimates of shape capture heritable variation which would be missed by linear estimates alone.

## 101 **Results**

102

### 103 *Variation in apple leaf shape*

104

105 We examined 24 phenotypes related to apple leaf shape and size including length, width, surface  
106 area, dry weight, leaf mass per area, within-tree variance, and overall shape estimated using PCs  
107 derived from EFD (elliptical Fourier descriptor) and PH (persistent homology) data (see  
108 Materials and Methods and Figure 1-2). The sample size and distribution of each phenotype, as  
109 well as the raw data, are provided (Figure S1; Table S1).

110

111 To visualize the primary axes of morphometric variation, we chose a representative leaf from  
112 accessions with the minimum and maximum values along the first 5 PCs for EFDs and PH  
113 (Figure 3a). The accessions with extreme values along PC1 for both methods are similar. In fact,  
114 ‘Binet Rouge’ has the lowest value along PC1 for EFD and PH, with the axis clearly

115 representing a decrease in the length-to-width (aspect) ratio. The annulus kernels most strongly  
116 contributing to PH PC1 (Figure S2) provide further evidence that this PC captures variation in  
117 aspect ratio. Variation in leaf shape captured by higher-order PCs is more complex and cryptic,  
118 and is thus not captured using linear measurements alone. In addition, while the primary axis of  
119 variation (PC1) using EFDs and PH may explain similar aspects of leaf morphology, the  
120 morphospaces resulting from the two techniques differ (Figure 3b).

121

122 **Figure 3. Examples of leaf shape across PCs derived from EFDs and PH.** Binary images of  
123 leaves from accessions with minimum and maximum values along PCs 1 to 5 for EFD and PH  
124 estimates. PCs were calculated using values estimated as the average across 8-10 leaves but only  
125 a single representative leaf is displayed. PCs were REML-adjusted based on tree position in the  
126 orchard. The accession name is also listed (a). Visualization of PC1 vs PC2 for EFD and PH  
127 data. Accession with minimum and maximum values along PC1 and PC2 are indicated (b).

128

129 Next, we examined the correlation between all measured traits (Table S3). By assessing the  
130 correlation of PCs resulting from a classical morphometric technique such as EFDs with a novel,  
131 topology-based morphometric approach like PH, we reveal how complementary the methods are  
132 (Figure 4; Figure S3). While there is a highly significant correlation between PC1 for both  
133 methods ( $R^2 = 0.949$ ,  $p < 1 \times 10^{-15}$ ), later PCs are often not significantly correlated, with the most  
134 notable exception being EFD PC2 and PH PC3 ( $R^2 = 0.432$ ,  $p < 1 \times 10^{-15}$ ), although several other  
135 PCs also show weak correlations. Thus, while the primary axis of variation (PC1) is consistent  
136 and highly correlated between methods, each method captures distinct aspects of leaf  
137 morphology in subsequent PCs.

138

139 **Figure 4. Correlations among leaf phenotypes.** Values above the diagonal are colored

140 according to the Pearson's correlation coefficient, and those below the diagonal indicate

141 Bonferroni-corrected p-values. The box enclosed by the dotted lines include comparisons only

142 between phenotypes captured by comprehensive morphometric analyses.

143

144 Many of the leaf phenotypes show a strong correlation with each other (Figure 4). In particular,

145 aspect ratio is highly correlated with PH PC1 ( $r = -0.878$ ,  $p < 1 \times 10^{-15}$ ), EFD PC1 ( $r = -0.855$ ,  $p$

146  $< 1 \times 10^{-15}$ ) and minor axis (leaf blade width) ( $r = -0.734$ ,  $p < 1 \times 10^{-15}$ ). The correlation between

147 the minor axis of a leaf and surface area ( $r = 0.939$ ,  $p < 1 \times 10^{-15}$ ) is higher than the correlation

148 between the major axis (blade length) and surface area ( $r = 0.810$ ,  $p < 1 \times 10^{-15}$ ). As expected,

149 leaf surface area is also highly correlated with average leaf dry weight ( $r = 0.934$ ,  $p < 1 \times 10^{-15}$ ),

150 indicating that larger leaves are heavier.

151

152 *Allometry in apple leaves*

153

154 The high correlation between aspect ratio and PC1 for both EFD and PH methods indicates that

155 length-to-width ratio is the primary source of variation in apple leaf shape. If there is an

156 allometric relationship between the minor and major axis, and thus, the length and width of a leaf

157 do not increase at equal rates, a slope significantly differing from 1 is expected. We find that the

158 slope between the two measurements is significantly greater than 1 (95% CI = 1.506-1.678,  $R^2 =$

159 0.343,  $p < 1 \times 10^{-15}$ ), indicating that the minor axis increases at a greater rate than the major axis.

160 While there is no significant correlation between the major axis (blade length) and EFD PC1 ( $R^2$

161 = 0.001,  $p = 1$ ) or PH PC1 ( $R^2 = 0.002$ ,  $p = 1$ ), there is a significant correlation for the minor axis  
162 (blade width) and EFD PC1 ( $R^2 = 0.541$ ,  $p < 1 \times 10^{-15}$ ) and PH PC1 ( $R^2 = 0.573$ ,  $p < 1 \times 10^{-15}$ )  
163 (Figure 5). As PC1 explains 80.23% of the variation in the leaf shape for EFDs, and 62.20% for  
164 PH, it is apparent that the width of the leaf blade, and not length, is the major source of leaf  
165 shape variation in apple. In fact, the aspect ratio, calculated as the ratio of major axis to minor  
166 axis, is even more strongly correlated with EFD and PH PC1, with an  $R^2$  of 0.732 for EFD PC1  
167 ( $p < 1 \times 10^{-15}$ ) and  $R^2$  of 0.771 for PH PC1 ( $p < 1 \times 10^{-15}$ ). Given the significant correlation  
168 between EFD PC1 and PH PC1 (Table S3), it is not surprising that aspect ratio is highly  
169 correlated with both.

170

171 **Figure 5. Correlation between the primary axis of variation (PC1) captured using EFD and**  
172 **PH values and leaf shape measures.** The EFD PC1 is plotted against the major axis (length of  
173 leaf blade) (a), minor axis (width of leaf blade) (b) and aspect ratio (ratio of length-to-width of  
174 blade) (c). The PH PC1 is plotted against the same measures in panels d-f. The percent variances  
175 explained by PC1, prior to REML-adjustment, is shown in parentheses. All p-values are  
176 Bonferonni-corrected based on the number of comparisons in Figure 4. A regression line from a  
177 linear model with a shaded 95% confidence interval is also shown.

178

179 In addition to variation between accessions, we investigated differences in leaf shape and size  
180 between species by comparing *Malus domestica*, the domesticated apple, with its primary  
181 progenitor species, *Malus sieversii* (Table S4). PCA of the genome-wide SNP data reveals a  
182 primary axis of genetic variation that separates *M. domestica* and *M. sieversii*, although  
183 separation is incomplete (Figure 6a). The major axis ( $p = 0.975$ ) of the leaves does not differ



184 between species (Figure 6b). However, the minor axis ( $p = 4 \times 10^{-4}$ ) of *M. domestica* leaves are  
185 significantly larger than *M. sieversii* (Figure 6c) and the aspect ratio ( $p = 0.023$ ) is significantly  
186 less (Figure 6d). Thus, there is allometric variation both within (Figure 5) and between (Figure 6)  
187 *Malus* species.

188

189 **Figure 6. Genetic and phenotypic comparison of the domesticated apple and its wild**

190 **ancestor.** PCs 1 and 2 were derived from 75,973 genome-wide SNPs and samples are labeled as  
191 *M. domestica* (purple), *M. sieversii* (green) or unknown (gray). *M. domestica* leaves do not differ  
192 from *M. sieversii* leaves along the major axis (b), but they have a larger minor axis (c) and aspect  
193 ratio (d). P-values reported are Bonferroni-corrected based on multiple comparisons (Table S4).  
194 Species labels are based on USDA classification.

195

196 *The genetic basis of leaf shape in apple*

197

198 GWAS of the 24 leaf phenotypes examined in this study yielded few significant results. We  
199 identified 70 significant SNPs representing 5 phenotypes which are reported in Table S5. We  
200 examined the regions surrounding significant SNPs for candidate genes using the GBrowse tool  
201 (Table S6) (22). We searched within a +/- 5,000 bp window, which should capture any linked  
202 causal variation given the rapid LD decay observed in a diverse collection of apples that is  
203 largely replicated in the germplasm studied here (23). However, no strong candidate genes were  
204 identified.

205

206 While GWAS examines the genome for single, large-effect loci, genomic prediction estimates  
207 our ability to predict a phenotype using genome-wide marker data. We complimented our  
208 GWAS with genomic prediction and observed prediction accuracies ( $r$ ) ranging from -0.10 to  
209 0.52 (Table S7; Figure S5a). Aspect ratio is the primary source of variation in leaf shape (Fig 5c)  
210 and it is also the leaf measurement that had the highest genomic prediction accuracy (0.52).  
211 Other phenotypes highly correlated with aspect ratio, such as leaf width (0.51), minor axis  
212 (0.49), EFD PC1 (0.48) and PH PC1 (0.47), all had relatively high prediction accuracies. PH  
213 PC3 (0.51) was also among the most well-predicted using genetic data.

214  
215 Similarly, estimates of narrow-sense heritability ( $h^2$ ) calculated using GCTA (24) ranged from 0  
216 to 0.75, with the highest heritability observed for aspect ratio (0.75) followed by leaf width  
217 (0.71), EFD PC1 (0.71), minor axis (0.69) and PH PC1 (0.65) (Figure 7; Table S8). Heritability  
218 estimates were highly correlated with genomic prediction accuracies (Figure S5b,  $R^2 = 0.936$ ,  $p$   
219  $< 1 \times 10^{-15}$ ), which is not surprising given that both techniques involve predicting a phenotype  
220 from genome-wide SNP data. None of the phenotypes measuring variance within the 8-10 leaves  
221 sampled had heritability estimates significantly different from 0.

222  
223 **Figure 7. Narrow-sense heritability ( $h^2$ ) of leaf phenotypes.** Values represent the additive  
224 genetic variance ( $V_g$ ) divided by the phenotypic variance ( $V_p$ ) with a standard error as calculated  
225 using GCTA (24). The dotted red lines are found at  $h^2 = 0$ , indicating that none of the phenotypic  
226 variance is explained by the genetic data. The proportion of the total phenotypic variance  
227 explained by each PC is indicated in parentheses.

228

229 While the principal component of variation in leaf shape detected by EFDs and PH is aspect  
230 ratio, we were also interested in determining if higher-order PCs, which capture variation not  
231 readily visible to the eye, are extracting information that is biologically meaningful. Using  
232 genomic prediction and heritability estimates, we found evidence of a genetic basis for these  
233 “hidden phenotypes”, which are unmeasurable using linear techniques. For example, the  
234 heritability of phenotypes such as PH PC6 (0.48), PH PC9 (0.35), PH PC10 (0.33) and EFD PC9  
235 (0.33) are similar to traditionally measured phenotypes such as leaf length (0.44) and leaf mass  
236 per area (0.40). While higher PCs may have relatively high heritability values, after a certain  
237 point the values (+/- standard error) overlap with 0, indicating that they are not heritable. The  
238 cutoff for morphometric PCs with a heritable genetic basis is approximately PC17. These results  
239 suggest that by making use of morphometric techniques that measure shape comprehensively, we  
240 are describing biologically meaningful, heritable phenotypes which would be missed by simple  
241 measurements such as leaf length, width and surface area.

242

## 243 **Discussion**

244

245 Leaf shape and size play a crucial role in the growth and development of apple trees, including  
246 the fruit. To elucidate the genetic basis of this variation, we quantified leaf shape in apple using  
247 traditional linear measurements and comprehensive morphometric techniques. Our work offers  
248 the first comparison between the novel topology-based technique, PH, and EFDs, which we find  
249 are complementary but distinct methods. For both methods, PC1 was highly correlated with the  
250 aspect ratio, thus providing evidence that the primary axis of variation in apple leaf shape can be  
251 captured using linear measurements. The minor axis, or width of the leaf blade, was also highly

252 correlated with PC1, while the major axis was not. Thus, variation in the aspect ratio is due to  
253 variation in the leaf blade width, not length. Leaf surface area was also more highly correlated  
254 with the minor axis than the major axis. Variation in leaf width is therefore essential to both the  
255 size and shape of apple leaves, similar to previous work in tomato (25).

256

257 The width of the leaf blade is not only the source of variation between apple accessions, but also  
258 between *M. domestica* and *M. sieversii*. The presence of the same allometric relationship within  
259 and between species suggests that the genetic loci controlling intra-specific leaf shape variation  
260 within *M. domestica* may be the same as those controlling the divergence in leaf shape observed  
261 between the domesticated apple and its wild ancestor. For example, in birds, while PC1 and PC2  
262 of bill shape explain the majority of variation across 2,000 species, they are also consistently  
263 associated with the variation between higher taxa (possessing >20 species) (26). Our results  
264 suggest that the increase in leaf size since domestication has not been an overall increase in leaf  
265 size but specifically an increase in blade width leading to larger leaves with a reduced length-to-  
266 width ratio.

267

268 Our work provides evidence that allometry is the primary source of morphometric variation in  
269 apple leaves. These findings are consistent with work reported in other species such as tomato,  
270 where the length-to-width ratio was the major source of shape variation (>40%) (5). Similarly,  
271 work in *Passiflora* and *Vitis* species performed using two independent morphometric techniques  
272 identified allometric variation as the primary source of variation in PC1, which explained at least  
273 40% of the variation in leaf shape (8, 27). Thus, linear measurements—in particular aspect  
274 ratio—are an important source of information when describing leaf shape. However, linear

275 measurements are not sufficient for capturing the full spectrum of diversity. In our study, PC1  
276 accounts for 62.20% or 80.23% of the variation, depending on the technique used. By simply  
277 quantifying apple leaves using linear measurements, we would miss nearly 40% of the variation  
278 in some cases. While PC1 is highly correlated with aspect ratio, later PCs represent orthogonal  
279 variation that can likely only be captured through morphometric techniques such as EFDs and  
280 PH. To fully quantify variation in leaf shape, comprehensive morphometric techniques are  
281 therefore essential.

282  
283 To discern the genetic contributions to leaf shape, we paired both linear and comprehensive  
284 morphometric estimates of shape with genome-wide SNP data. There are examples of a simple  
285 genetic basis of leaf shape, such as in *Arabidopsis thaliana*, where the *ANGUSTIFOLIA* and  
286 *ROTUNDIFOLIA3* independently control leaf width and length (28). In barley, transcript levels  
287 of *BFL1* limit leaf width, with overexpression resulting in narrower leaves and loss of *BFL1*  
288 function resulting in a reduced length-to-width ratio (29). Using GWAS, we found no robust  
289 associations with shape phenotypes, observed a low ratio of significant SNPs to the number of  
290 phenotypes examined, and found that significant SNPs were sparsely distributed across multiple  
291 chromosomes. In addition, the small number of significant SNPs are likely spurious associations  
292 due to poor correction for cryptic relatedness, as evidenced by the QQ plots (Fig S4). These  
293 observations suggest that leaf shape is likely polygenic and controlled by a large number of small  
294 effect loci, such as in tomato and maize (5, 21). In comparison, GWAS on apple fruit  
295 phenotypes, such as color and firmness, have revealed strong associations resulting from a small  
296 number of large effect loci (23). However, it is possible that large effect loci were missed in the  
297 present study, either because of poor reference genome assembly or inadequate marker density.

298 Improvements in genome assembly and increases in marker number will aid to further reveal the  
299 genetic architecture of apple leaf shape variation.

300

301 Lastly, we investigated the degree to which leaf shape is heritable and can be predicted using  
302 genome-wide SNP data. We find that the genomic prediction accuracies of the primary axes of  
303 leaf shape variation are similar to previously reported estimates for fruit width (0.48) and length  
304 (0.47), indicating that leaf shape is as heritable as fruit shape (23). In combination with few  
305 significant GWAS results, high narrow-sense heritability estimates support a polygenic basis for  
306 leaf shape. Aspect ratio was identified as the primary source of variation in leaf shape in apple  
307 and had the highest genomic prediction and heritability estimates, indicating that there is a  
308 genetic, heritable basis for allometric variation in apple. While we did not detect a genetic basis  
309 for leaf shape variation within an accession, we intentionally sampled leaves representing the  
310 mean of a tree, and this may have diminished power. Further, although the first 5 PCs for both  
311 EFDs and PH explain the majority of the variation in apple leaf shape, most PCs from 1 to 14  
312 have heritability estimates above 0.20 and may still represent crucial differences in leaf shape  
313 from an ecological, evolutionary, or agricultural perspective. Thus, while our ability to detect the  
314 primary axes of variation in leaf shape using genome-wide data is expected, our observation that  
315 higher level PCs are also heritable confirms that these comprehensive morphometric methods  
316 capture biologically meaningful variation that would be missed by linear measurements alone.

317

## 318 **Conclusions**

319

320 It is clear from our work that variation in apple leaf shape and size are under genetic control.  
321 Further, high genomic prediction and heritability estimates for higher morphometric PCs indicate  
322 that techniques such as EFDs and PH are capturing heritable biological variation that will be  
323 missed if researchers restrict leaf shape estimates to linear measurements. Based on these results,  
324 it may be possible to perform genomic selection for a phenotype that could only be detected  
325 using morphometrics. If a higher order PC was correlated with a trait that was difficult or  
326 expensive to measure, assessing leaf shape could potentially be used as proxy for that phenotype,  
327 in the same manner that red leaf color can be used to select for red fruit flesh color in apples (13,  
328 14). Additionally, a better understanding of the variation in leaf shape and size in apple could  
329 ultimately have important implications for canopy management, where light exposure is crucial  
330 to flowering (17). Ultimately, through the first in-depth study of leaf shape in apple, we uncover  
331 allometry between accessions and species, as well as evidence that complex and heritable  
332 phenotypes can be captured using comprehensive morphometric techniques.

333

## 334 **Materials and Methods**

335

### 336 *Sample collection*

337

338 Apple trees in Kentville, Nova Scotia, Canada were budded onto M.9 rootstocks in spring 2012.

339 In the fall, the trees were uprooted and kept in cold storage until spring 2013, when trees were

340 planted in an incomplete block design (see “REstricted Maximum Likelihood (REML)” below).

341 Leaves from over 900 trees were collected from August 24th to September 16th 2015. Ten leaves

342 were collected from each tree. Leaves were flattened and placed to avoid touching, then scanned

343 using Canon CanoScan (LiDE 220) Colour Image Scanners. Leaves were then dried for 48 hours  
344 at 65 °C and weighed to estimate the total dry weight (g) for each tree.

345

#### 346 *Morphometric analyses*

347

348 Leaf scans were converted into a separate binary image for each leaf using custom ImageJ  
349 macros, which included the ‘make binary’ function (30). A new image file was created for each  
350 leaf and named after the tree ID. Images were converted to RGB .bmp files and a chain code  
351 analysis was performed using SHAPE (31). The chain code was used to calculate normalized  
352 elliptical Fourier descriptors (EFDs) in SHAPE. The normalized EFDs were read into Momocs  
353 v1.1.5 (32) in R (33) where harmonics B and C were removed to eliminate asymmetrical  
354 variation in leaf shape.

355

356 The binary leaf images were also analyzed using persistent homology (PH) (10). To numerically  
357 estimate the shape of the leaves using PH, we extracted the leaf contour using a 2D point cloud  
358 (Figure 1a). After centering and normalizing the contour to its centroid size, we used a Gaussian  
359 density estimator (Figure 1b), which assigns high values (red) to pixels with many neighboring  
360 pixels, and low values (blue) to pixels with fewer neighboring pixels. We multiplied the density  
361 estimator by an annulus kernel, or ring (Figure 1c), which emphasizes the shape in an annulus at  
362 the centroid and is thus invariant to orientation (Figure 1d). The resulting function can also be  
363 visualized from the side view (Figure 1e,f). As we moved a plane from top to the bottom, we  
364 recorded the number of connected components above the plane, forming a curve. With each new  
365 component this value increased, and each time components were merged, it decreased (Fig 1g).



366 For each leaf, we computed 16 curves corresponding to 16 expanding rings. For computational  
367 purposes, each curve is divided into 500 numbers, ultimately resulting in the shape of each leaf  
368 being represented by 8,000 (16\*500) values.

369

370 **Figure 1. Visualization of persistent homology technique for annulus kernel 7.** Binary  
371 images were converted into a 2D point cloud (a) which was then normalized using a Gaussian  
372 density estimator (b). For each leaf, 16 annulus kernels were used. Annulus kernel 7, indicated in  
373 purple (c) is used as an example for this visualization. The density estimator is multiplied by ring  
374 7 (d). The function can also be visualized from the side view (e, f). As a plane moves from top to  
375 bottom, the number of connected components is recorded along the curve (g). Below (g) are five  
376 visualizations of curves that are represented as red vertical dotted lines in (g).

377

378 Only leaves for which both EFDs and PH shape estimations were successfully calculated were  
379 included in subsequent analyses. Additionally, only trees with 8-10 leaves were included, as  
380 leaves were sometimes removed due to tears, folding, or the absence of a petiole which did not  
381 allow for accurate quantification of shape. The final dataset consisted of 915 trees with 8-10  
382 leaves, which included 869 unique accessions and 8,995 leaves.

383

384 EFDs and PH values were averaged across leaves from an individual tree. The contribution of  
385 EFD harmonics 1 to 15 to the mean leaf shape across all trees was visualized using the ‘hcontrib’  
386 function in the Momocs R package (Figure 2). To allow for discrimination between accessions  
387 based on leaf shape, principal component analysis (PCA) was performed using the Momocs  
388 ‘PCA’ function (32) for EFDs, and the ‘prcomp’ function in R for PH values, which center but

389 do not scale the data. The resulting PC values were adjusted using REstricted Maximum  
390 Likelihood (see below). Subsequently, we identified the accession with the minimum and  
391 maximum value along each of the first 5 PCs.

392

393 **Figure 2. Contribution of elliptical Fourier descriptor harmonics to leaf shape.** The leaf  
394 shapes depicted are the mean leaf shapes based on all 915 trees. Harmonics 1 to 15 are  
395 represented on the x-axis and each harmonic is multiplied by the amplification factor on the y-  
396 axis to visualize their contribution to mean leaf shape. An amplification factor of 0 indicates the  
397 removal of the harmonic; a factor of 1 results in the normal shape; and values above 1 exaggerate  
398 effects to better visualize the harmonic's contribution to the final shape.

399

400 In addition to estimating the contour of the leaf using EFDs and PH, we used several more  
401 metrics to describe the leaves. Using ImageJ, we automated the measurement of leaf surface area  
402 ( $\text{cm}^2$ ), length (cm) of the leaf and width (cm) of the leaf as well as major (blade length) and  
403 minor (blade width) axes of the best fitting ellipse—which excluded the petiole—through batch  
404 processes (30). Throughout the manuscript, we use ‘major’ when referring to the length of the  
405 leaf blade, and ‘minor’ when referencing the width of the leaf blade. We also calculated the  
406 aspect ratio of the leaf, by dividing the major axis by the minor axis. Additionally, leaf mass per  
407 area was calculated for 780 trees where we possessed surface area data for all 10 leaves, by  
408 calculating the ratio of dry weight to surface area ( $\text{g}/\text{cm}^2$ ).

409

410 While linear phenotypes were calculated as an average value for a particular tree, we also  
411 estimated variance within a tree for aspect ratio, length, width, major and minor axis, and surface

412 area. Variance was calculated as the coefficient of variation using the ‘cv’ function in the raster  
413 package (34) in R to estimate within-tree variability in leaf size, which is indicated as ‘var’  
414 throughout this manuscript.

415

416 *REstricted Maximum Likelihood (REML) adjustment of phenotype data*

417

418 The orchard sampled in this study is an incomplete block design with 1 of 3 standards per grid.  
419 The standards, or “control trees”—‘Honeycrisp’, ‘SweeTango’, and ‘Ambrosia’—are replicated  
420 across the grid. Leaves from these trees were sampled multiple times across the orchard, which  
421 allowed us to correct for positional effects. Each phenotype was adjusted using a REstricted  
422 Maximum Likelihood (REML) model which resulted in one adjusted value per accession, even  
423 when multiple trees were measured. The impact of row grid (rGrid), column grid (cGrid) and  
424 rGrid x cGrid effects were adjusted for using the following REML model:

425

$$phenotype \sim accession + (1 | rGrid) + (1 | cGrid) + (1 | cGrid:rGrid)$$

426

427 We fit a linear mixed-effects model via REML using the ‘lmer’ function in the lme4 package in  
428 R (35) and then calculated the least squares means using the ‘lsmeans’ function in the lsmeans R  
429 package (36).

430

431 Thus, while the initial phenotype data was collected for 915 trees, following REML adjustment,  
432 one value remained per unique accession, resulting in 869 accessions. REML-adjustment was  
433 applied directly to all size, weight and variance estimates. For PH and EFDs, we applied the

434 REML following PCA and thus the percent contribution for each PC was calculated using  
435 unadjusted values. The adjusted data for all 24 phenotypes are included in Table S1.

436

#### 437 *Phenomic analyses*

438

439 The correlation between leaf phenotypes was calculated using Pearson's correlation and p-values  
440 were Bonferroni-corrected for multiple comparisons. The resulting heatmap was visualized using  
441 the 'geom\_tile' function in ggplot2 in R (37). Next, we examined the leaves for allometry using  
442 the 'SMA' function in the smartr R package (38) to estimate if the slope between the log-  
443 transformed minor and major axis differed from 1.

444

445 Accessions were labelled as either *Malus x. domestica* Borkh. or *Malus sieversii* Lebed. based on  
446 information provided by the United States Department of Agriculture (USDA) Germplasm  
447 Resources Information Network website (<http://www.ars-grin.gov/>) (Table S2). We used a  
448 Mann-Whitney U test to test if any phenotypes differed between species and Bonferroni-  
449 corrected all p-values for multiple comparisons.

450

#### 451 *Genomic analyses*

452

453 DNA was extracted using commercial extraction kits. Genotyping-by-sequencing (GBS) libraries  
454 were prepared using ApeKI and PstI-EcoT221I restriction enzymes according to Elshire, *et al.*  
455 (39). GBS libraries were sequenced using Illumina Hi-Seq 2000 technology. Reads which failed  
456 Illumina's "chastity filter" were removed from raw fastq files. Remaining reads were aligned to

457 the *Malus x. domestica* v1.0 pseudo haplotype reference sequence (40) using the Burrows-  
458 Wheeler aligner tool v0.7.12 (41) and the Tassel version 5 pipeline (42). Tassel parameters  
459 included a minKmerL of 30, mnQS of 20, mxKmerNum of 50000000 and batchSize of 20. The  
460 kmerlength was set to 82 for ApeKI and 89 for PstI-EcoT22I based on the max barcode size. The  
461 minMAF for the DiscoverySNPCallerPluginV2 was set to 0.01. All other default parameters  
462 were used. Non-biallelic sites and indels were removed using VCFtools v.0.1.14 (43). VCFs for  
463 both enzymes were then merged using a custom perl script, preferentially keeping SNPs called  
464 by PstI-EcoT22I at overlapping sites, since those sites tended to be at higher coverage.

465  
466 Missing data was imputed using LinkImputeR v0.9 (Money et al., Submitted, available:  
467 <http://www.cultivatingdiversity.org/software.html>) with global thresholds of 0.01 for minor allele  
468 frequency (MAF) and 0.70 for missingness. We examined depths of 3 to 8 and selected a case  
469 for imputation with a max position/sample missingness of 0.70, a minimum depth of 5, and an  
470 imputation accuracy of 94.9%. The VCF was converted to a genotype table using PLINK v1.07  
471 (44, 45).

472  
473 Of the 869 accessions assessed in this study, 816 had genomic data following imputation and  
474 filtering and were included in downstream analyses. The resulting genotype table consisted of  
475 816 accessions and 197,565 SNPs. Subsequently, a 0.05 MAF filter was applied using PLINK,  
476 after which 128,132 SNPs remained. SNPs with more than 90% heterozygous genotypes were  
477 removed. The final genotype table consisted of 816 samples and 122,596 SNPs.

478

479 To perform PCA, SNPs were pruned for linkage disequilibrium (LD) using PLINK. We  
480 considered a window of 10 SNPs, removing one SNP from a pair if  $R^2 > 0.5$ , then shifting the  
481 window by 3 SNPs and repeating (PLINK command: indep-pairwise 10 3 0.5). This resulted in a  
482 set of 75,973 SNPs for 816 accessions. PCA was performed on the LD-pruned genome-wide  
483 SNPs using ‘prcomp’ in R with data that were centered but not scaled. The first 2 genomic PCs  
484 were visualized using ggplot2 in R (37).

485

486 We performed a genome-wide association study (GWAS) using the mixed linear model in Tassel  
487 (version 5) for each phenotype, adjusting for relatedness among individuals using a kinship  
488 matrix as well as the first 3 PCs for population structure (46, 47). The threshold for significance  
489 was calculated using simpleM (48, 49) which estimates the number of PCs needed to explain  
490 0.995 of the variance, or the number of independent SNPs. The inferred  $M_{eff}$  used to calculate  
491 the significance threshold was 91,667 SNPs.

492

493 We searched the regions surrounding any significant GWAS SNPs using the Genome Database  
494 for Rosaceae GBrowse tool for *Malus x. domestica* v1.0 p genome (22). We used a window of  
495 +/- 5,000 bp (10 kb) surrounding the significant SNP to check for genes, and when identified, we  
496 used the basic local alignment search tool (BLAST) from NCBI to search for the mRNA  
497 sequence and reported the result with the max score (50).

498

499 Genomic prediction was performed using the ‘x.val’ function in the R package PopVar (51). The  
500 rrBLUP model was selected and 5-fold (nFold=5) cross-validation was repeated 3 times  
501 (nFold.reps=3) with no further filtering (min.maf=0) from the set of 122,596 SNPs used for

502 GWAS. All other default parameters were used. In addition to performing genomic prediction on  
503 the main 24 phenotypes examined in this study, we performed genomic prediction on all 40 PCs  
504 for EFDs and on the first 40 PCs for PH values. We also used the ‘rnorm’ function in R to  
505 generate 1,000 random phenotypes with a mean of 0 and a standard deviation of 1, and  
506 performed genomic prediction using these random phenotypes to obtain the range of genomic  
507 prediction accuracies one can expect at random. Lastly, we used genome-wide complex trait  
508 analysis (GCTA) v.1.26.0 which estimates the genetic relationships between individuals based  
509 on genome-wide SNPs and uses this information to calculate the variance explained by these  
510 SNPs. The ratio of additive genetic variation to phenotypic variance is used to calculate narrow-  
511 sense heritability ( $h^2$ ), or SNP heritability, of a trait (24). We used GCTA to estimate heritability  
512 for each phenotype, including the first 40 PCs for EFD and PH. We also estimated the  
513 correlation between genomic prediction accuracy ( $r$ ) and narrow-sense heritability ( $h^2$ ) using a  
514 Pearson’s correlation.

515

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517

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524

525 **Supplementary Material**

526 **Figure S1. Distribution of leaf phenotypes following REML-adjustment.** N is equal to the  
527 total number of unique samples.

528 **Figure S2. Visualization of contributions of each ring to PH PC1.** Rings 6, 7 and 16  
529 contribute the most to leaf shape according to PH PC1. The placement of each ring is visualized  
530 on a leaf representing the minimum and maximum value along PC1 (a). The contribution to PC1  
531 of each of the 16 rings is also shown (b).

532

533 **Figure S3. Comparison of morphometric EFD and PH PCs 1 to 5.** Correlation between first 5  
534 PCs, estimated using Pearson's correlation, including  $R^2$  and Bonferroni corrected p-values  
535 based on Figure 4/Table S3.

536

537 **Figure S4. GWAS results for all 24 leaf phenotypes examined.** Manhattan and QQ plots are  
538 included for each phenotype. The QQ-plot shows both the results of a naive GWAS (Pearson  
539 correlation) and the results from applying the mixed model. P-values are log-transformed and the  
540 threshold for significance is simpleM-corrected and indicated by a horizontal dotted line.  
541 Chromosome R indicates SNPs found on contigs unanchored to the reference genome.

542

543 **Figure S5. Genomic prediction accuracy ( $r$ ) (a) and correlation between genomic prediction  
544 results and narrow-sense heritability estimates ( $h^2$ ) for all leaf phenotypes (b).** Genomic  
545 prediction accuracies represent the average correlation (+/- standard deviation) between observed  
546 and predicted phenotype scores, based on 5-fold cross-validation with 3 iterations. Dotted red  
547 lines indicate the minimum and maximum prediction average accuracy ( $r$ ) achieved using 1,000



548 randomly generated phenotypes. The percent variance explained by each PC was calculated prior  
549 to REML-adjustment and is indicated in parentheses.

550

551 **Table S1. All leaf phenotypes assessed in apple, following REML-adjustment.** Accessions  
552 are identified by their unique “apple id”. Further information about these accessions is available  
553 in Table S2.

554

555 **Table S2. Metadata for all accessions assessed in this study.** In addition to the unique numeric  
556 apple\_id, we report the Germplasm Origin (where budwood was obtained from) and Species  
557 (*Malus domestica*/*Malus sieversii*).

558

559 **Table S3. Correlation between leaf phenotypes as well as Bonferroni-adjusted p-values.**  
560 Pearson's product moment correlation coefficients are reported. These results are visualized in  
561 Figure 2.

562

563 **Table S4. Comparison of leaf phenotypes between accessions based on metadata.**  
564 Bonferroni-adjusted p-values resulting from a Mann-Whitney U test estimating the difference  
565 between accessions based on species (*Malus domestica*/*Malus sieversii*) for the leaf phenotypes  
566 examined.

567

568 **Table S5. Positional information for significant GWAS results.** Additional information about  
569 significant SNPs are included such as p-value, marker  $R^2$ , minor and major allele, minor and  
570 major effect and MAF.

571

572 **Table S6. Genes found within +/- 5 kb of SNPs with significant associations to phenotypes**

573 **from GWAS.** Results are listed according to the Genome Database for Rosaceae GBrowse

574 (accessed January 27 2017). Overlapping mRNA, length, contig, GO category, GO term

575 accession, GO term name, InterPro Term, InterPro Description and NCBI sequence with Max

576 Score when BLASTed using NCBI are reported.

577

578 **Table S7. Genomic prediction accuracies (r) for leaf phenotypes.**  $r_{avg}$  represents the

579 average correlation between observed and predicted phenotype scores, based on 5-fold cross-

580 validation with 3 iterations. The standard deviation ( $r_{sd}$ ) is also reported.

581

582 **Table S8. Narrow-sense heritability ( $h^2$ ) for leaf phenotypes.**  $h^2$  represents the genetic

583 variance ( $V_g$ ) divided by the phenotypic variance ( $V_p$ ). The standard error (SE) is also reported.

584 These results are visualized in Figure 7.

585

## 586 **References**

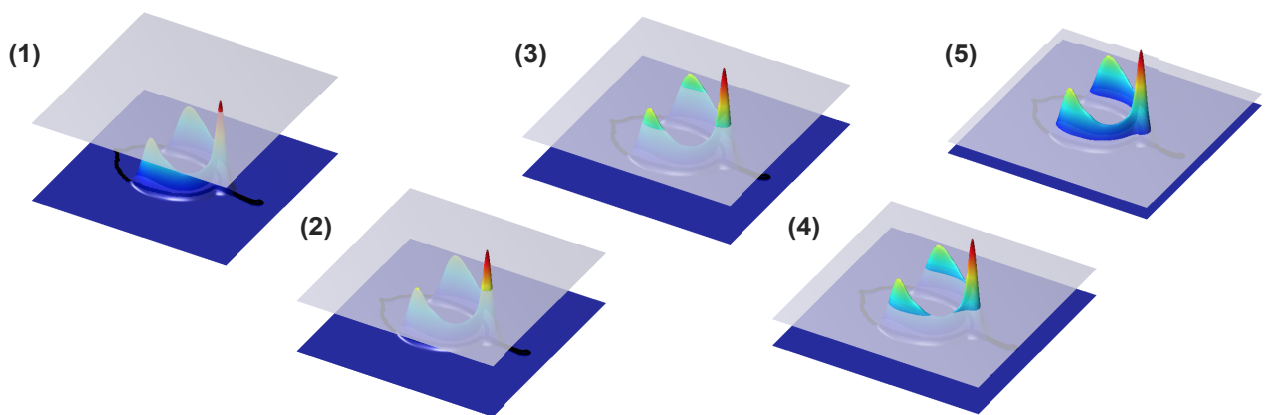
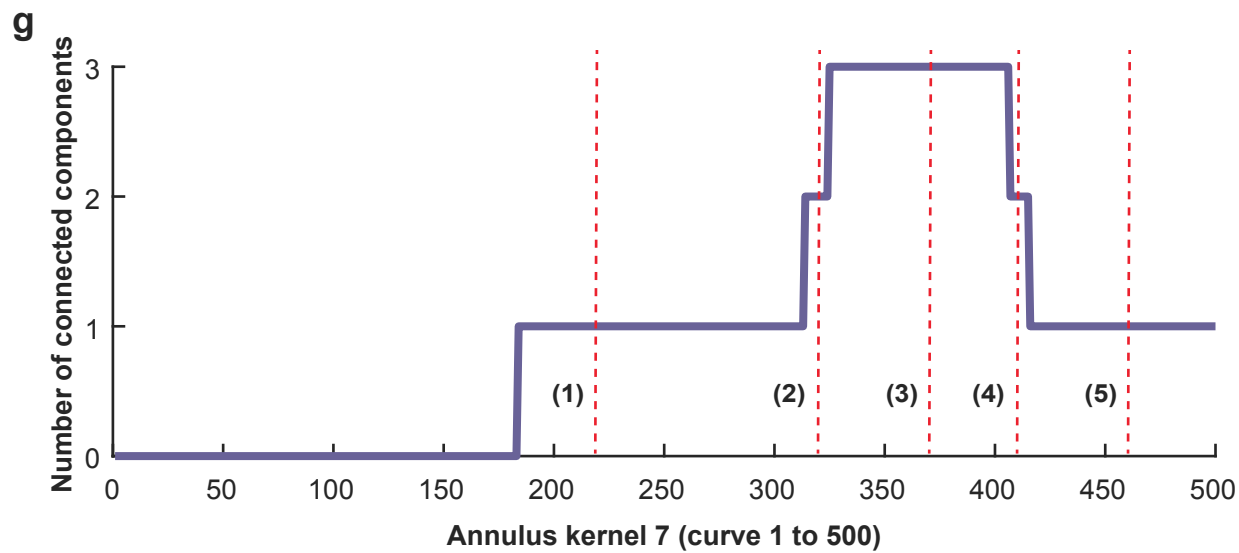
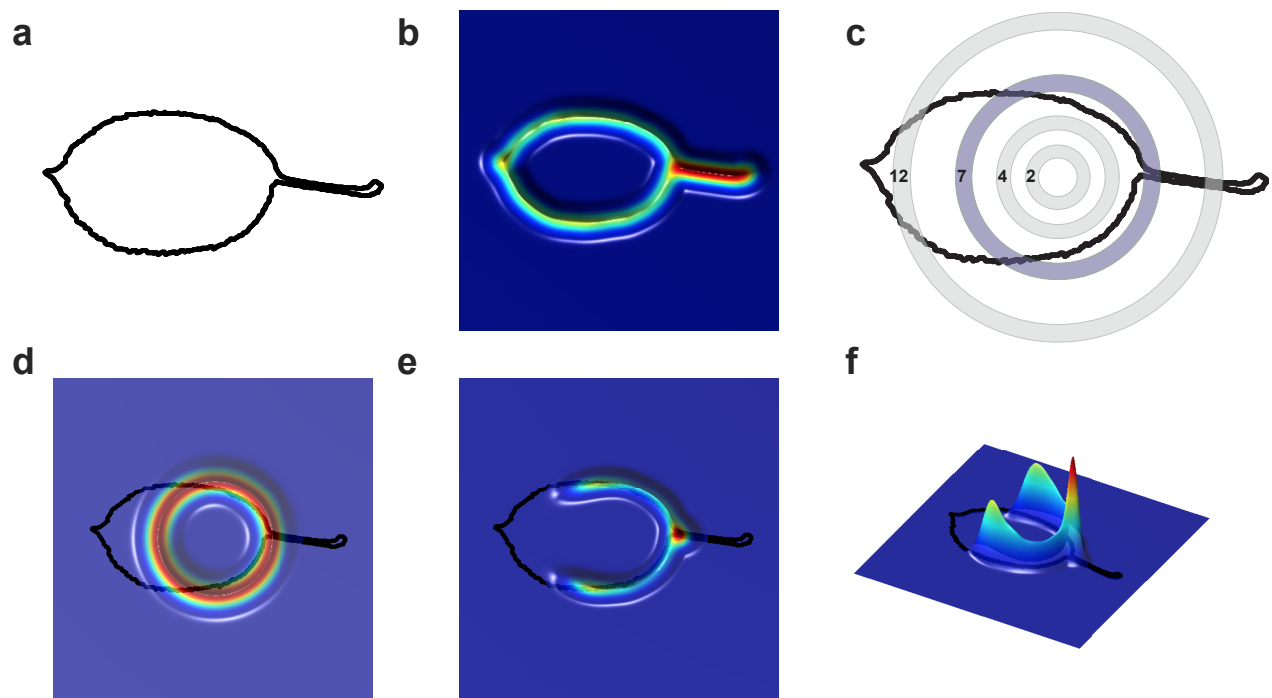
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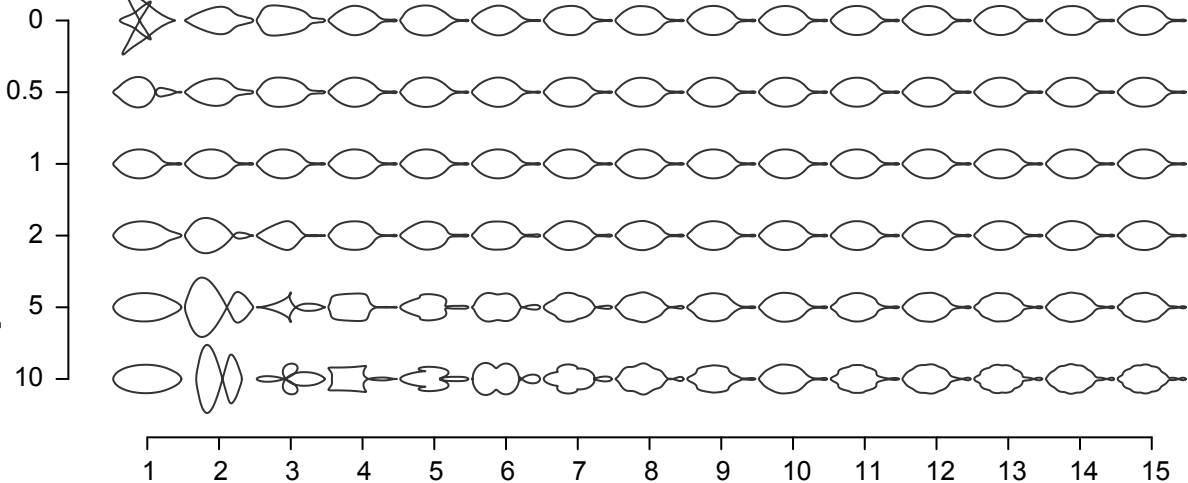
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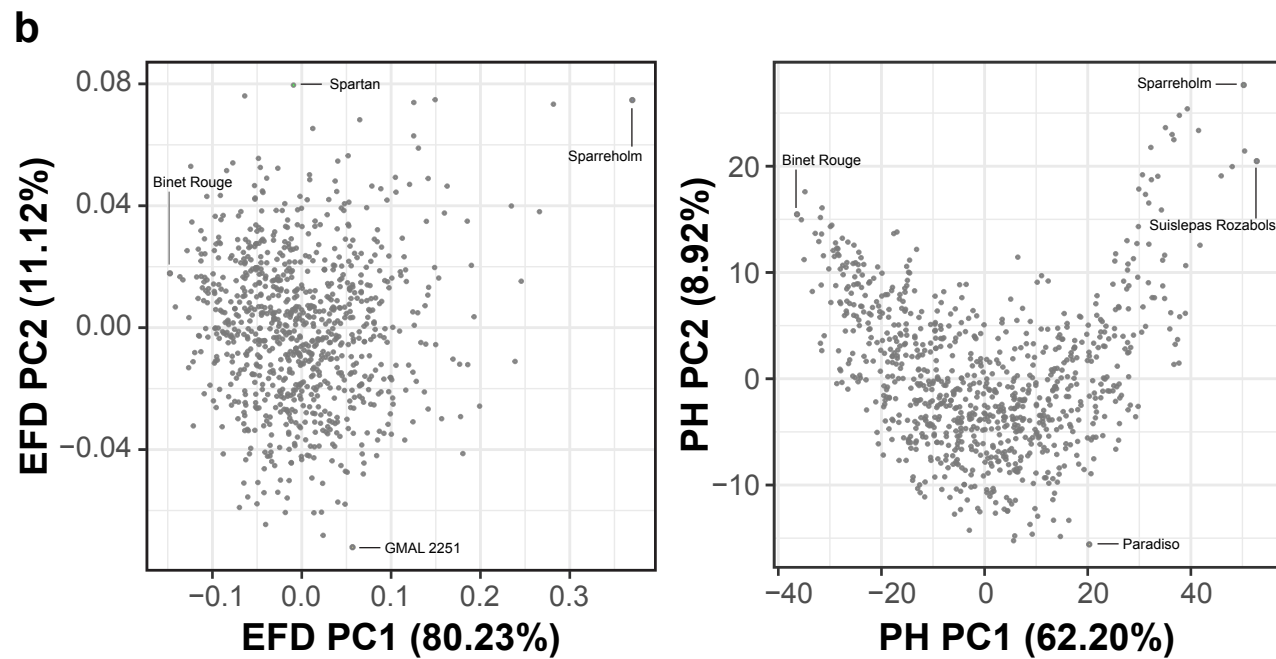
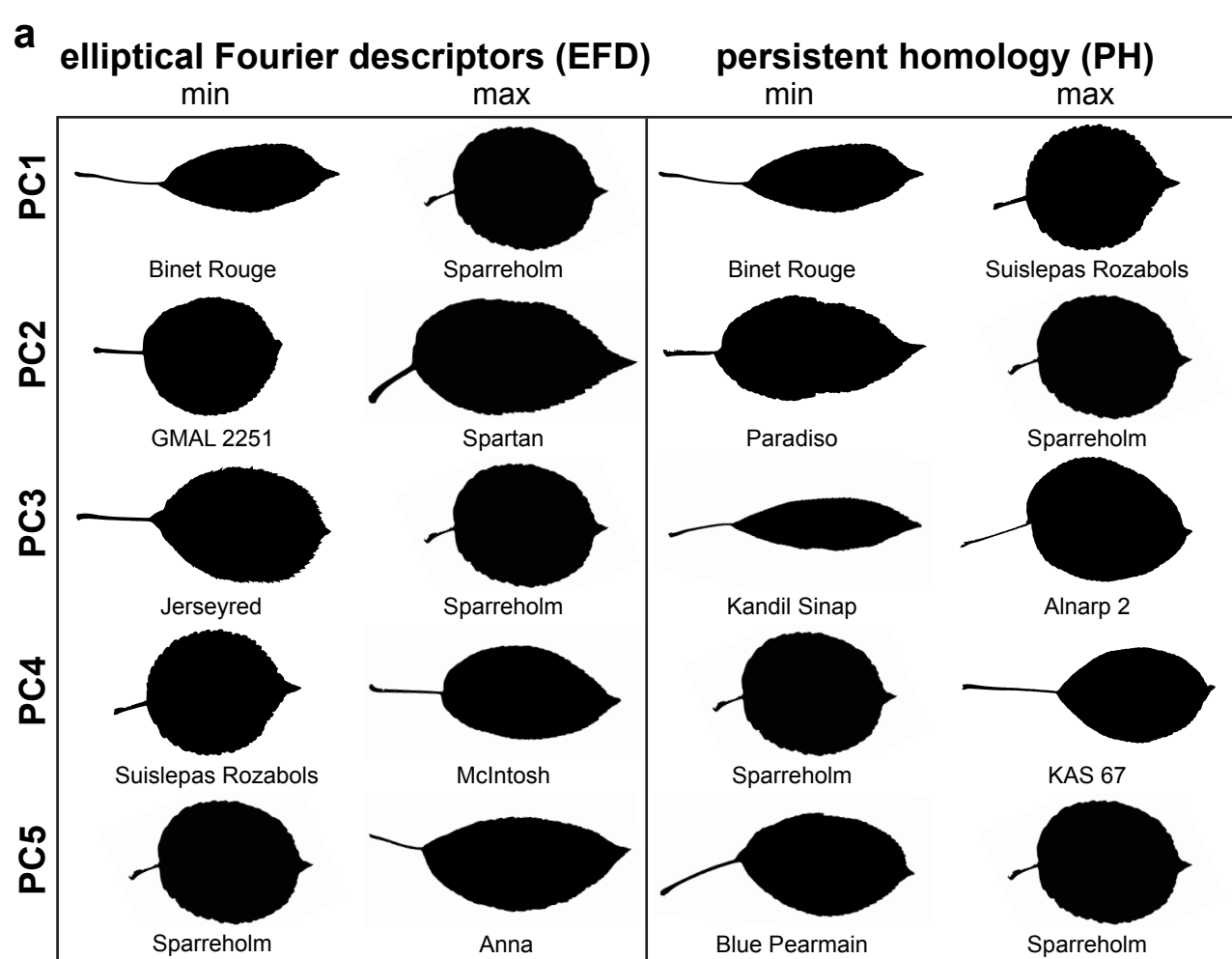
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**Amplification factor**

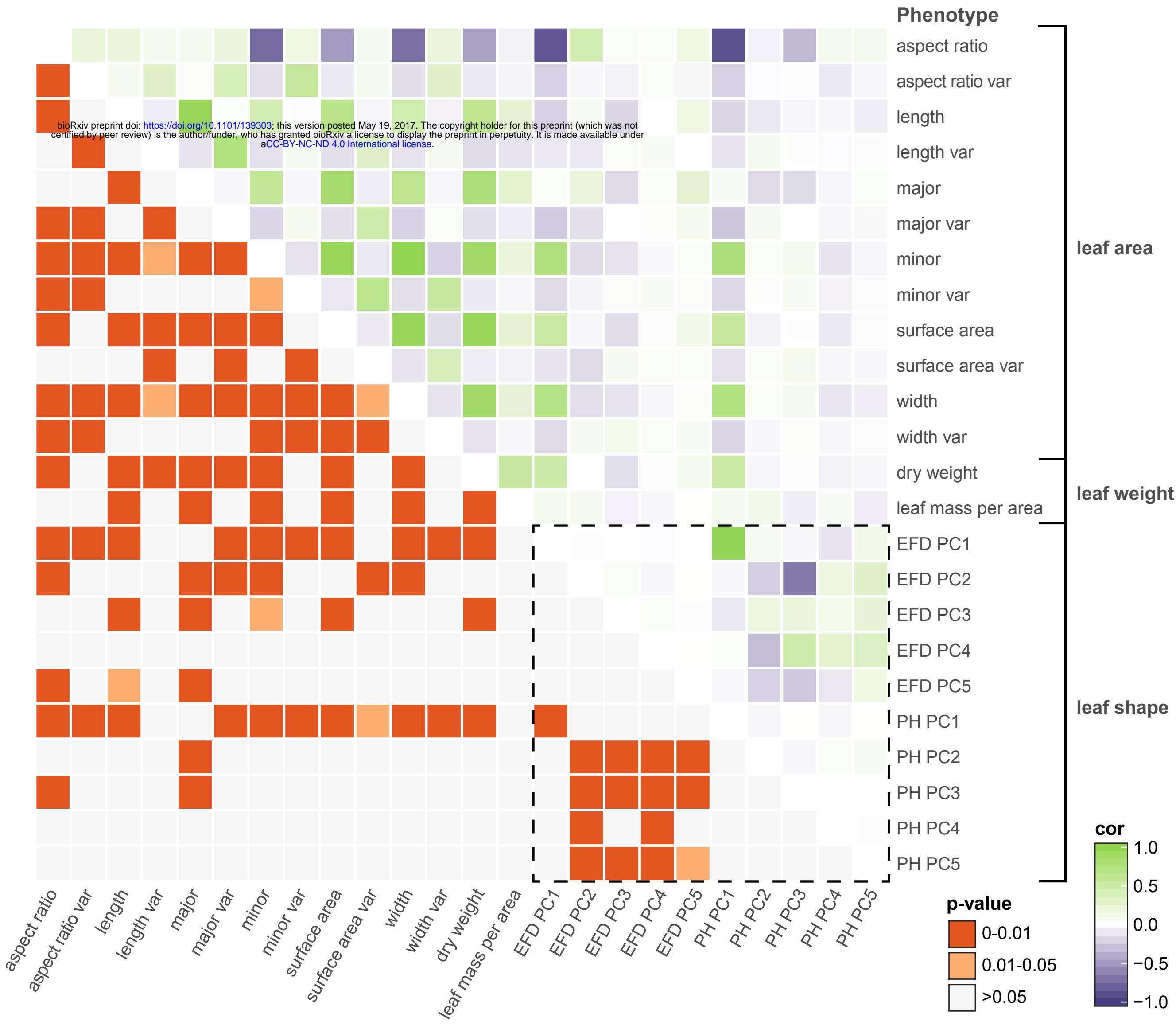


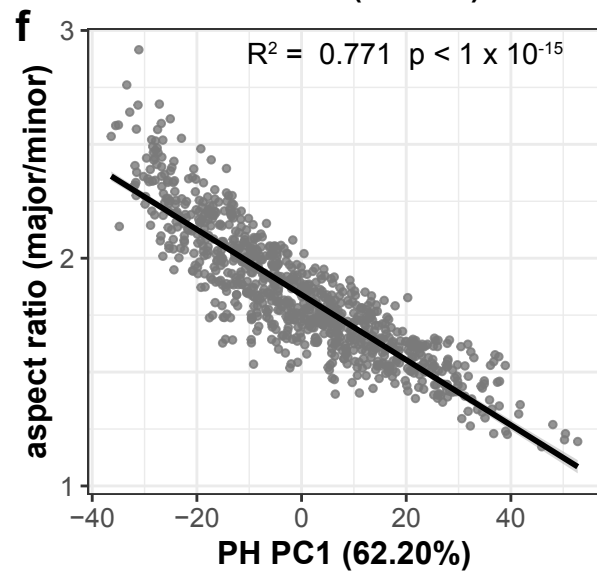
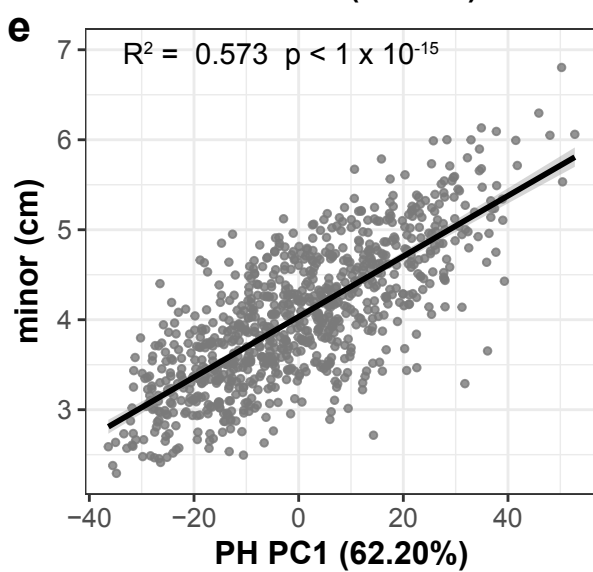
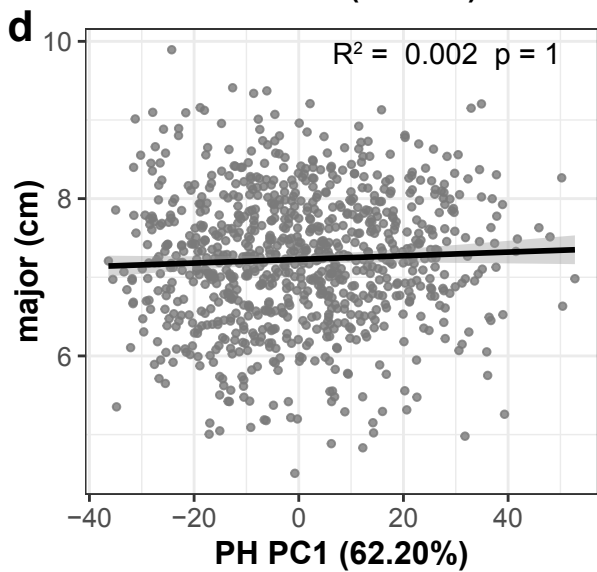
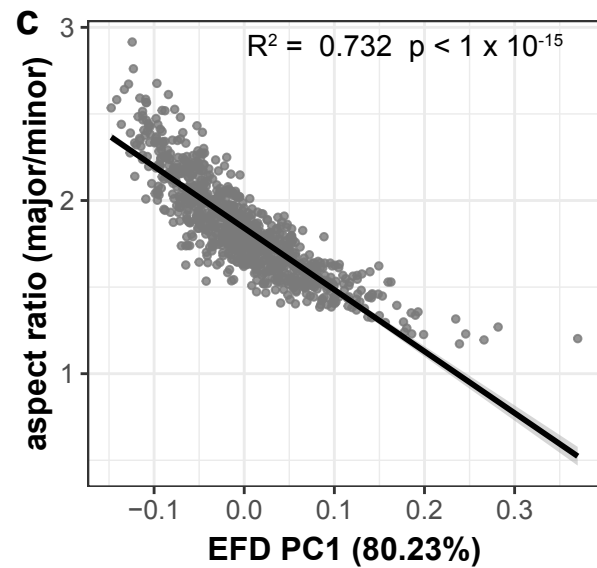
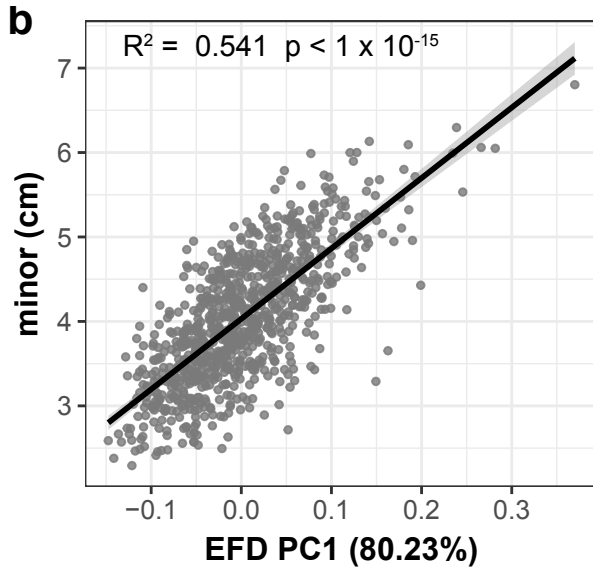
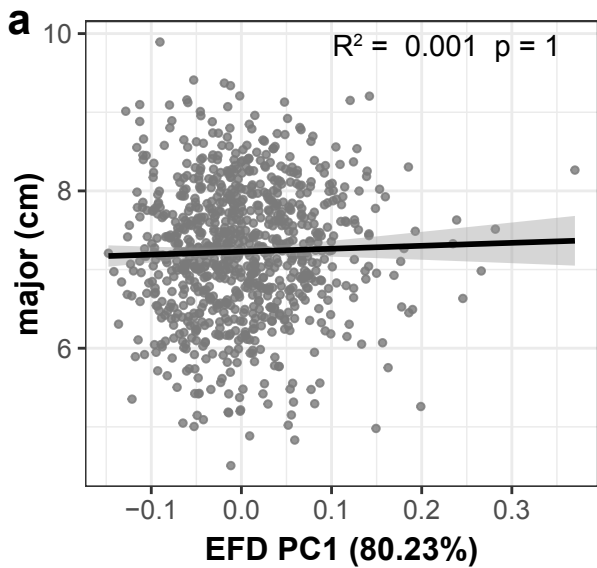
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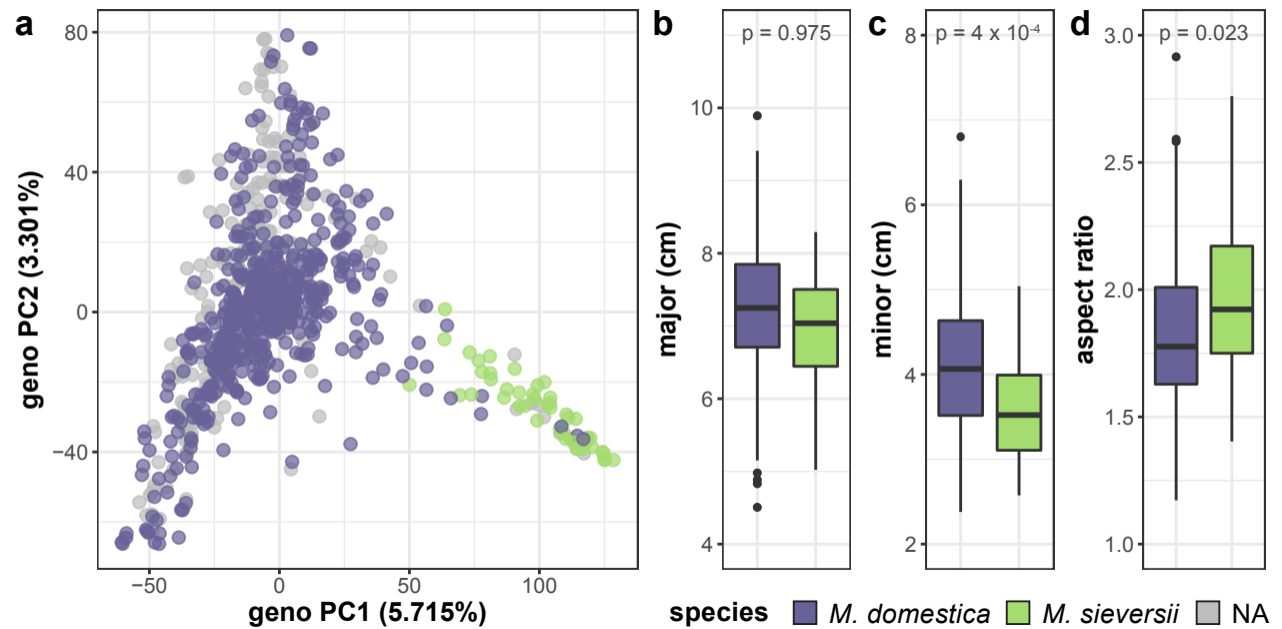




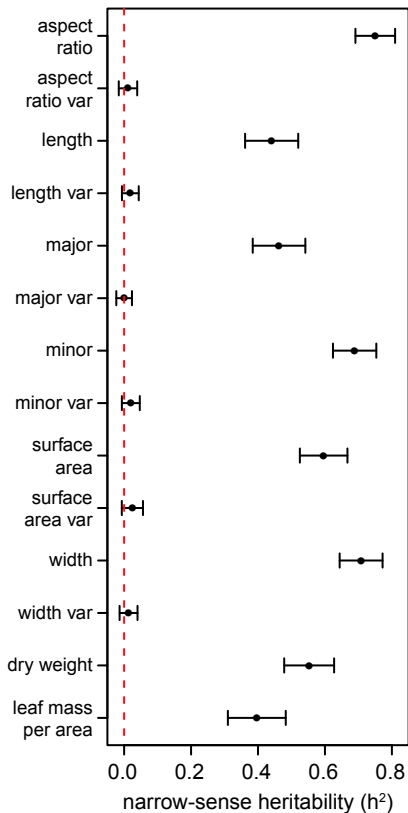
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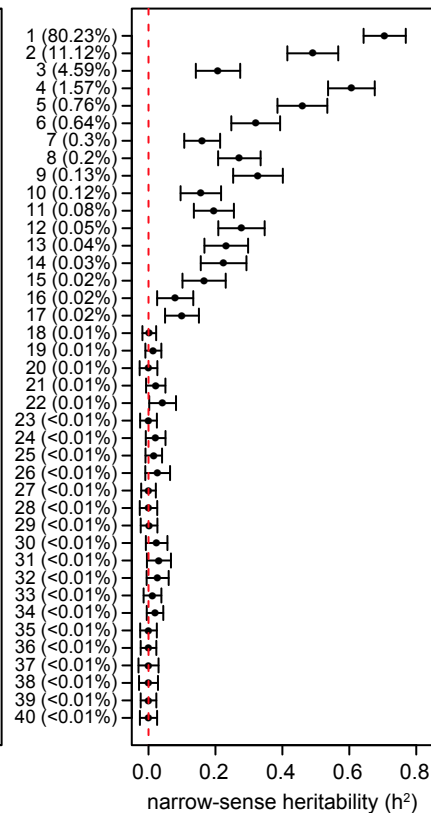




leaf area and weight



elliptical Fourier descriptors (EFD) PCs



persistent homology (PH) PCs

